

## Number Types

An **integer** is any whole number, negative or positive. For example, 56 or -56 is an integer.

A **rational number** is one that can be expressed in the form  $\frac{p}{q}$  where  $p$  and  $q$  are both integers and  $q \neq 0$ . For example,  $-4$  is a rational number since it can be expressed as  $\frac{-4}{1}$ . Another rational number could be 9.5 which can be expressed as  $\frac{19}{2}$ . An **irrational number** is one that can not be expressed in the above form. Probably the most cited irrational numbers are  $\pi$  and  $\sqrt{2}$ .

$\Re$  stands for the space of real numbers. A **real number** can be absolutely any number that is not a complex number. Thus a real can be a decimal or a whole number, an irrational or a rational number; negative or positive. In linear algebra there is extensive use of vectors in different  $\Re$ -dimensions.

A **vector** is simply a list of numbers. Sometimes they are called column vectors which captures more precisely their appearance. They have an  $m \times 1$  dimension; this means that the vectors are of  $m$  rows ( $m$  can be any positive integer) but only one column. A vector in  $\Re^2$  (read as “R-two”) is a  $2 \times 1$  matrix such as  $\mathbf{v} = \begin{bmatrix} 3 \\ 4 \end{bmatrix}$ . The exponent in  $\Re$  indicates the number of rows in the vector.  $\Re^7$  is a vector with 7 rows.

A **complex number** is an expression that is made up of a “real” element and an “imaginary” element. Some example of complex numbers are  $1 + i$  or  $-2 + i\sqrt{3}$ . The first part is the “real” element and the second part is the “imaginary” element whereby  $i$  is multiplied by a real. “ $i$ ” stands for imaginary ( $i = \sqrt{-1}$ ). The space of complex numbers is denoted by  $\mathbb{C}$ .