



Workshop on Monetary Policy in Developing Economies  
Istanbul School of Central Banking

# **Monetary Policy, Capital Flows, and Exchange Rates**

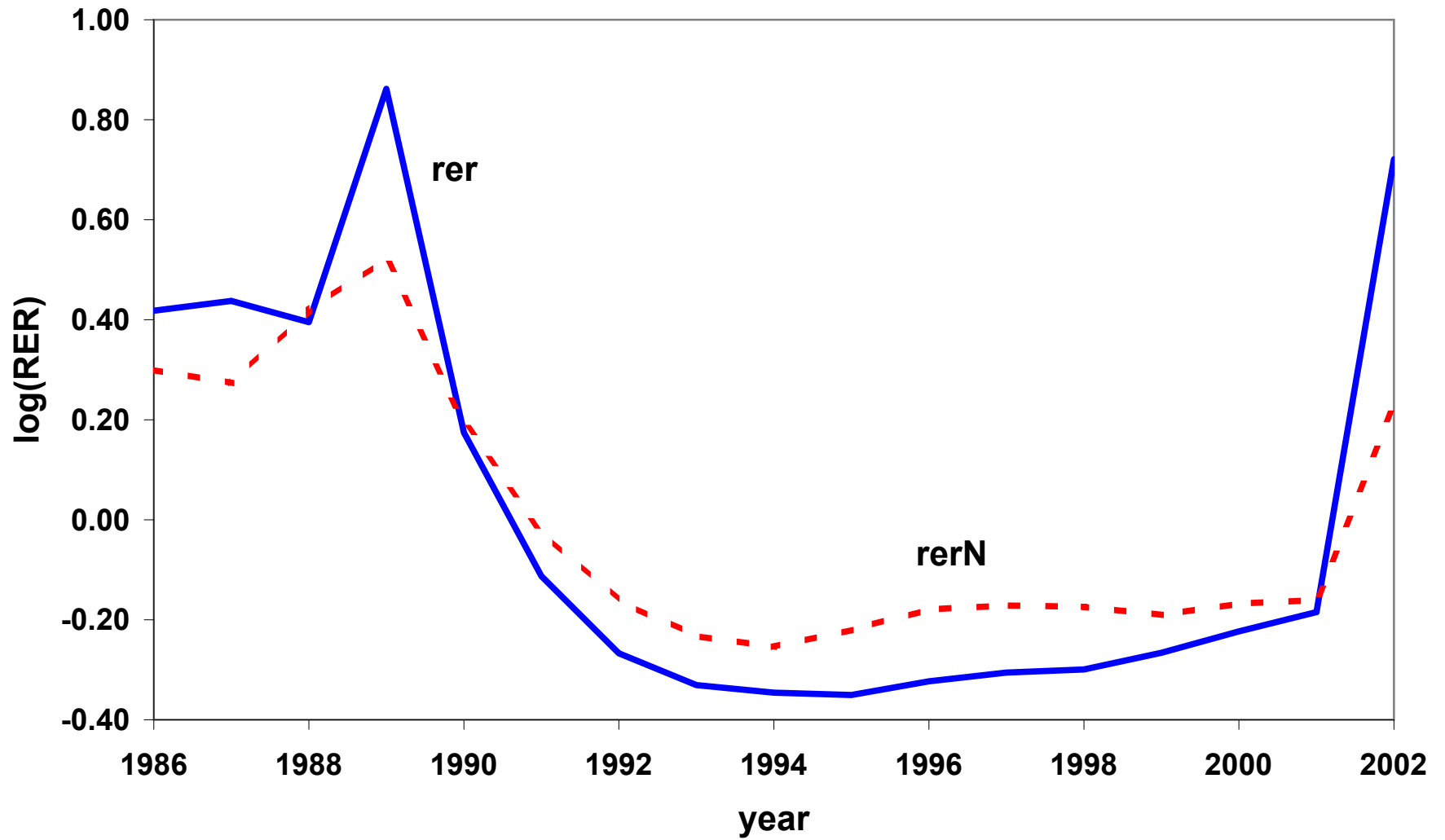
## **Part 1: Exchange Rates and Monetary Policy**

Timothy J. Kehoe

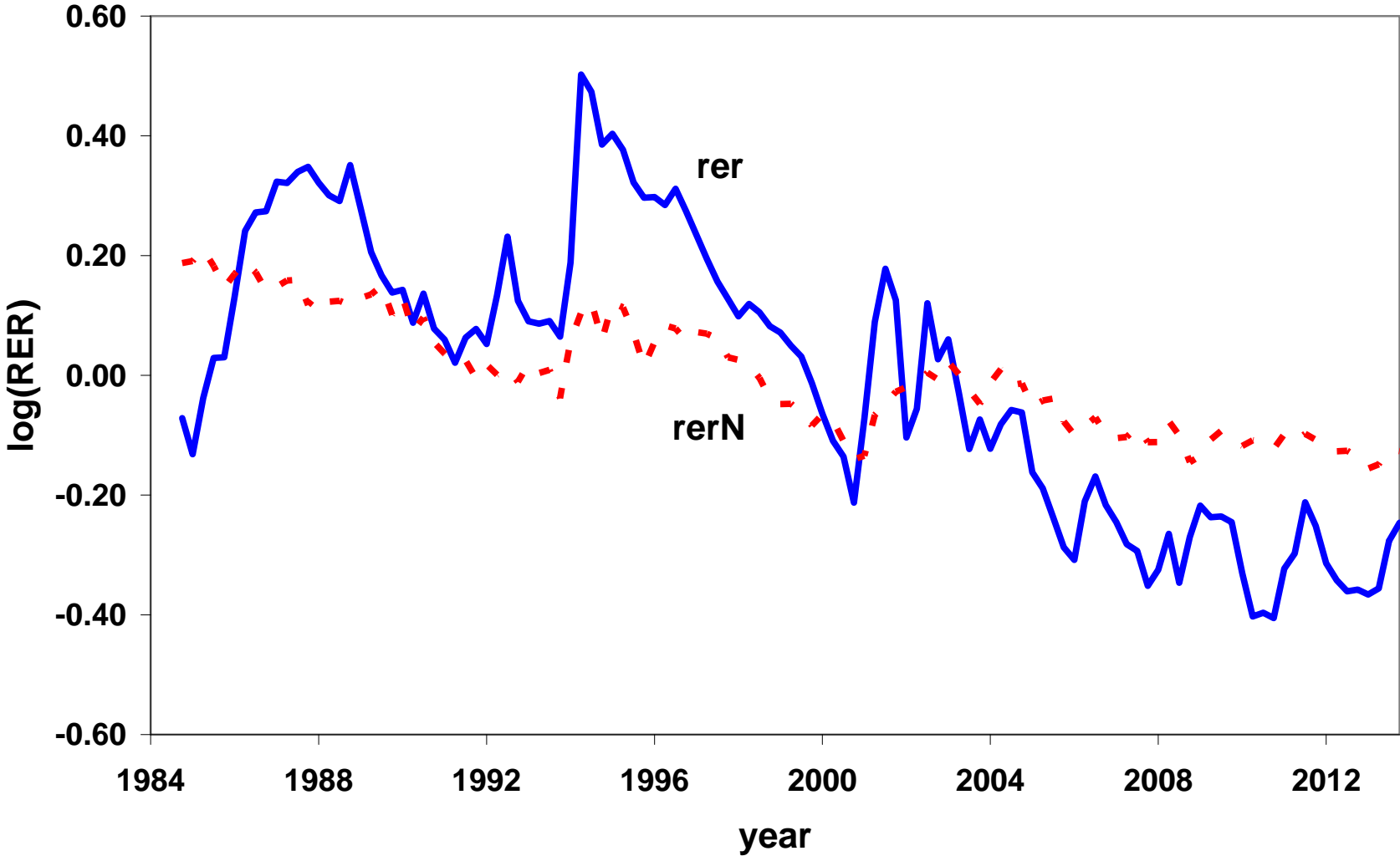
University of Minnesota and Federal Reserve Bank of Minneapolis

May 2014

## Argentina-U.S. Real Exchange Rate



# Turkey-Germany Real Exchange Rate



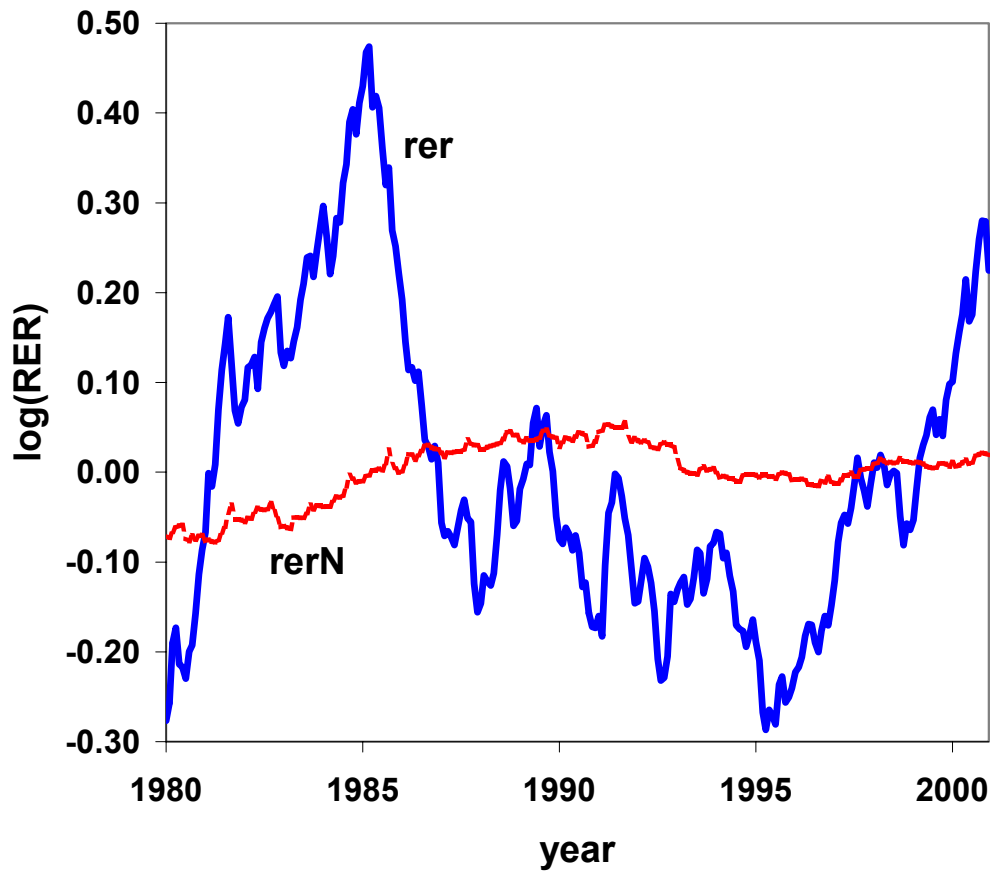
# **TRADABILITY OF GOODS AND REAL EXCHANGE RATE MOVEMENTS**

**Timothy J. Kehoe and Caroline M. Betts**

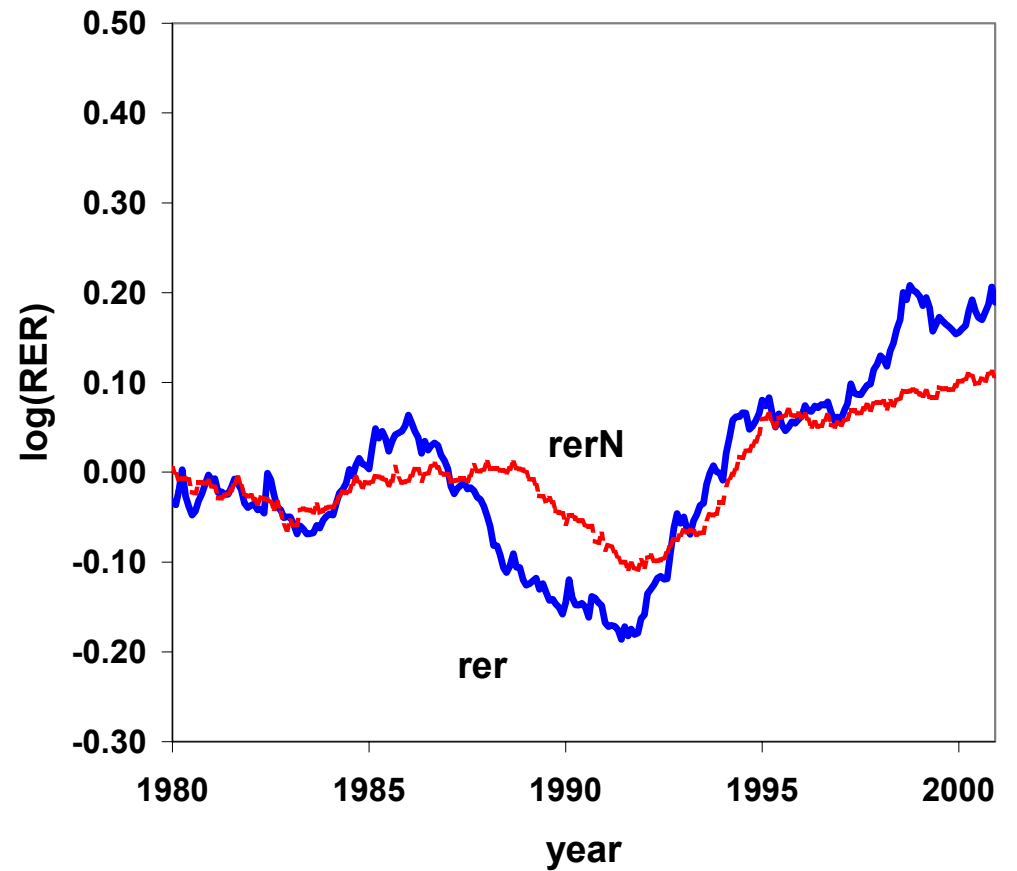
1. “U.S. Real Exchange Rate Fluctuations and Relative Price Fluctuations”
2. “Real Exchange Rate Movements and the Relative Price of Nontraded Goods”
3. “Tradability of Goods and Real Exchange Rate Fluctuations”

# U.S. BILATERAL REAL EXCHANGE RATES AND RELATIVE PRICES OF NONTRADED GOODS

## Germany-U.S. Real Exchange Rate Monthly CPI/PPI



## Canada-U.S. Real Exchange Rate Monthly CPI/PPI



We investigate the empirical relation between

the U.S. bilateral real exchange rate with 5 of her largest trade partners

and

the bilateral relative price of nontraded to traded goods.

We measure the relation by

simple correlation (comovements)

relative standard deviation (volatility)

variance decompositions (percent of fluctuations)

We find the relation depends crucially on

1. the price series used to measure the relative price of nontraded goods
2. the choice of trade partner.

Specifically, the relation is stronger when

1. traded goods prices are measured using production site prices  
— not final consumption price data
2. the trade intensity between the U.S. and a trade partner is larger  
— links international relative price behavior and size of trade flows

Traditional theory real exchange rate theory (Cassel, Pigou, and many others)

dichotomy of goods into

- costlessly traded (arbitraged prices)
- entirely nontraded (domestic prices)

**INAPPROPRIATE**



# **PLAN OF DISCUSSION**

- Methodology
- Data
- Results
- What We Learn
- Extended Results (paper 2)
- Theoretical Model (paper 3)
- Conclusions

## **METHODOLOGY**

Traditional real exchange rate theory attributes all (or most) real exchange rate movements to changes in the relative price of nontraded goods.

Recent empirical analyses using variance decompositions argue there is almost no role for relative price of nontraded goods in real exchange rate movements. All movements are driven by deviations from law of one price.

# REAL EXCHANGE RATE MEASUREMENT

Bilateral real exchange rate between the United States and country  $i$ :

$$RER_{i,us} = NER_{i,us} \frac{P_{us}}{P_i}$$

$NER_{i,us}$ : nominal exchange rate — country  $i$  currency units per U.S. dollar

$P_j$ : price deflator or index for the basket of goods consumed or produced in country  $j$ ,  $j = us, i$ .

Traditional theory dichotomizes goods into

- costlessly traded (arbitraged prices)
- entirely nontraded (domestic prices)

$$P_j(P_j^T, P_j^N)$$

Decompose

$$RER_{i,us} = \left( NER_{i,us} \frac{P_{us}^T}{P_i^T} \right) \left( \frac{P_i^T}{P_i} / \frac{P_{us}^T}{P_{us}} \right)$$

$$RER_{i,us} = RER_{i,us}^T \times RER_{i,us}^N$$

where

$$RER_{i,us}^T = NER_{i,us} \frac{P_{us}^T}{P_i^T}$$

is the real exchange rate of traded goods — the component that measures deviations from the law of one price and

$$RER_{i,us}^N = \left( \frac{P_i^T}{P_i(P_i^T, P_i^N)} \right) / \left( \frac{P_{us}^T}{P_{us}(P_{us}^T, P_{us}^N)} \right)$$

is what we refer to as the (bilateral) relative price of nontraded (to traded) goods.

In logarithms,

$$rer_{i,us} = rer_{i,us}^T + rer_{i,us}^N.$$

In the case where

$$P_j(P_j^T, P_j^N) = (P_j^T)^{\gamma_j} (P_j^N)^{1-\gamma_j},$$

$$\begin{aligned} RER_{i,us}^N &= \left( \frac{P_i^T}{P_i(P_i^T, P_i^N)} \right) / \left( \frac{P_{us}^T}{P_{us}(P_{us}^T, P_{us}^N)} \right) \\ &= \left( \frac{P_i^T}{(P_i^T)^{\gamma_i} (P_i^N)^{1-\gamma_i}} \right) / \left( \frac{P_{us}^T}{(P_{us}^T)^{\gamma_{us}} (P_{us}^N)^{1-\gamma_{us}}} \right) \\ &= \left( \frac{P_i^T}{P_i^N} \right)^{1-\gamma_i} / \left( \frac{P_{us}^T}{P_{us}^N} \right)^{1-\gamma_{us}} \end{aligned}$$

## SUMMARY STATISTICS

Analyze the relation between  $rer_{i,us}$  and  $rer_{i,us}^N$ :

$$1. \quad \text{corr}(rer_{i,us}, rer_{i,us}^N) = \frac{\text{cov}(rer_{i,us}, rer_{i,us}^N)}{\left(\text{var}(rer_{i,us})\text{var}(rer_{i,us}^N)\right)^{1/2}}.$$

$$2. \quad \frac{\text{std}(rer_{i,us}^N)}{\text{std}(rer_{i,us})} = \left(\frac{\text{var}(rer_{i,us}^N)}{\text{var}(rer_{i,us})}\right)^{1/2}$$

$$3. \quad \text{vardec}(rer_{i,us}, rer_{i,us}^N) = \frac{\text{var}(rer_{i,us}^N)}{\text{var}(rer_{i,us}^N) + \text{var}(rer_{i,us}^T)}$$

(Another possibility:

$$\text{vardec}^2(rer_{i,us}, rer_{i,us}^N) = \frac{\text{var}(rer_{i,us}^N) + \text{cov}(rer_{i,us}^N, rer_{i,us}^T)}{\text{var}(rer_{i,us})}.)$$

# DATA

Data on 5 of largest trade partners of the United States:

- Canada (1)
- Mexico (2)
- Japan (3)
- Germany (6)
- Korea (7).

These countries account for 53 percent of U.S. trade in 2000.



Construct measures of  $rer_{i,us}$ :

Need aggregate price indices (and nominal exchange rates)

1. Deflator for Gross Output at production site for all goods and services produced by a country (GO)
2. Consumer Price Index for entire basket of consumption goods and services (CPI)
3. Personal Consumption Deflators for all personal consumption expenditures (PCD).

(Another possibility: Deflator for Gross Domestic Product for all goods and services produced by a country (GDP).)

Construct measures of  $rer_{i,us}^N$ :

Need traded goods price measures

1. Deflator for GO of agriculture, mining, and manufacturing
2. Producer price index for entire basket of producer goods (PPI).
3. CPI for “traded” components of consumption basket - all goods less food.
4. PCD for “traded” components of personal consumption expenditures - commodities.

(Another possibility: Deflator for GDP of agriculture, mining, and manufacturing.)

## WHAT WE LEARN

- The frequency of the data does not matter.
- Detrending matters (theory should guide for the choice and the explanation for why it matters).
- The size of bilateral trade relationship is crucial.

The larger is the trade relationship, the more closely related are  $rer_{i,us}$  and  $rer_{i,us}^N$ .

- The data series used to measure the relative price of nontraded goods  $rer_{i,us}^N$  matters a lot.

**good conceptually**  
sectoral GO deflators  
PPIs

**not good conceptually**  
CPI components  
PCD components  
(sectoral GDP deflators)

**highly correlated**  
CPI components-PCD components  
sectoral GOP deflators-PPIs (-sectoral GDP deflators)

**widely available**  
PPIs

**less widely available**  
CPI components  
PCD components  
(sectoral GDP deflators)

**difficult to obtain**  
sectoral GO deflators

## **SUGGESTION**

**MODIFY THE TRADITIONAL THEORY SO  
THAT GOODS DIFFER BY DEGREE OF  
TRADABILITY**

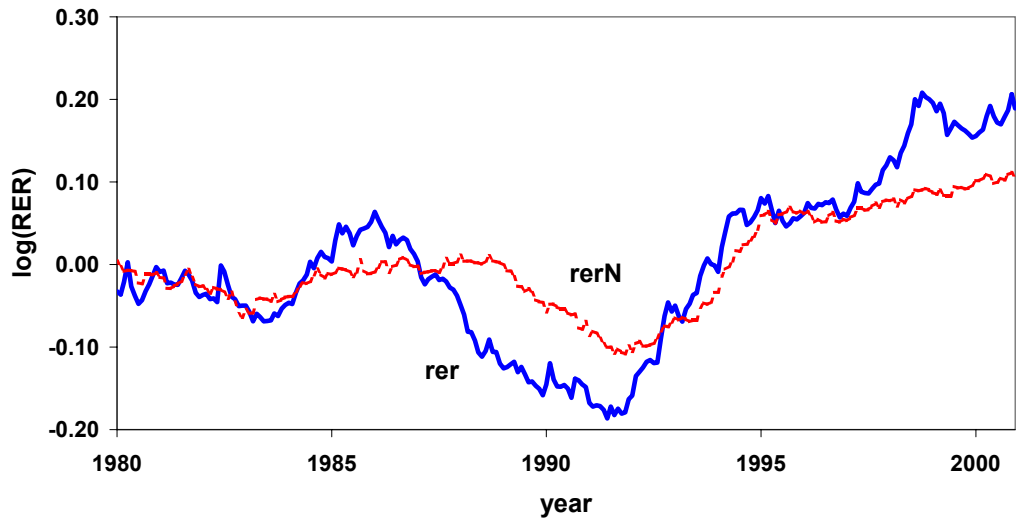
TABLE 1

**COMPARISON OF FREQUENCIES:  
CANADA-U.S. REAL EXCHANGE RATE  
PPI-CPI data 1980-2000**

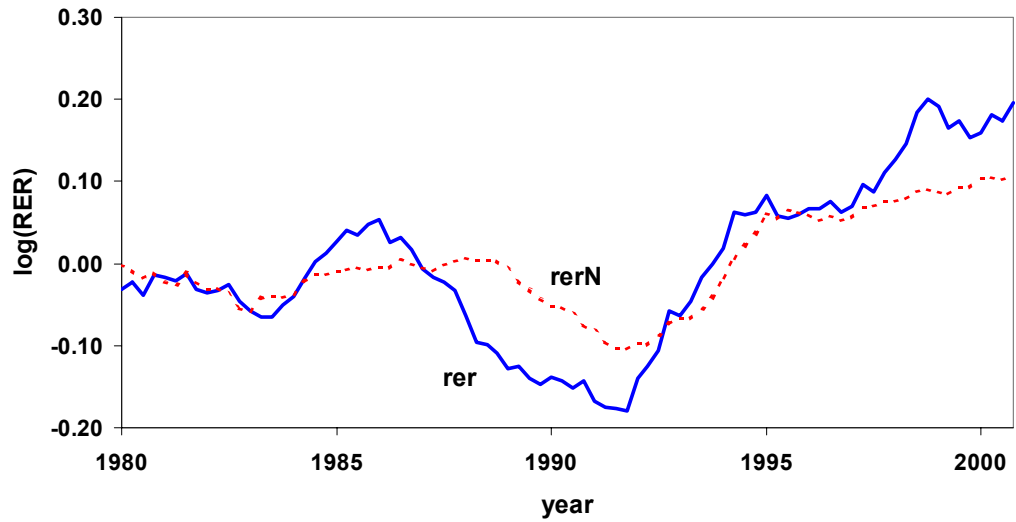
	annual	annual	quarterly	quarterly	quarterly	monthly	monthly	monthly	monthly
Levels									
<b>corr(rer,rer<sup>N</sup>)</b>	0.88		0.88			0.88			
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.70		0.69			0.69			
<b>vardec(rer,rer<sup>N</sup>)</b>	0.66		0.65			0.65			
Detrended levels									
<b>corr(rer,rer<sup>N</sup>)</b>	0.88		0.88			0.87			
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.51		0.51			0.51			
<b>vardec(rer,rer<sup>N</sup>)</b>	0.41		0.41			0.41			
Changes	1 lag (1 year)	4 lags (4 years)	1 lag (1 quarter)	4 lags (1 year)	16 lags (4 years)	1 lag (1 month)	3 lags (1 quarter)	12 lags (1 year)	48 lags (4 years)
<b>corr(rer,rer<sup>N</sup>)</b>	0.70	0.82	0.56	0.70	0.82	0.48	0.48	0.67	0.82
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.55	0.55	0.51	0.55	0.55	0.55	0.51	0.55	0.55
<b>vardec(rer,rer<sup>N</sup>)</b>	0.40	0.51	0.28	0.39	0.51	0.29	0.26	0.37	0.50

# CANADA-U.S. REAL EXCHANGE RATE

## Monthly CPI/PPI



## Quarterly CPI/PPI



## Annual CPI/PPI

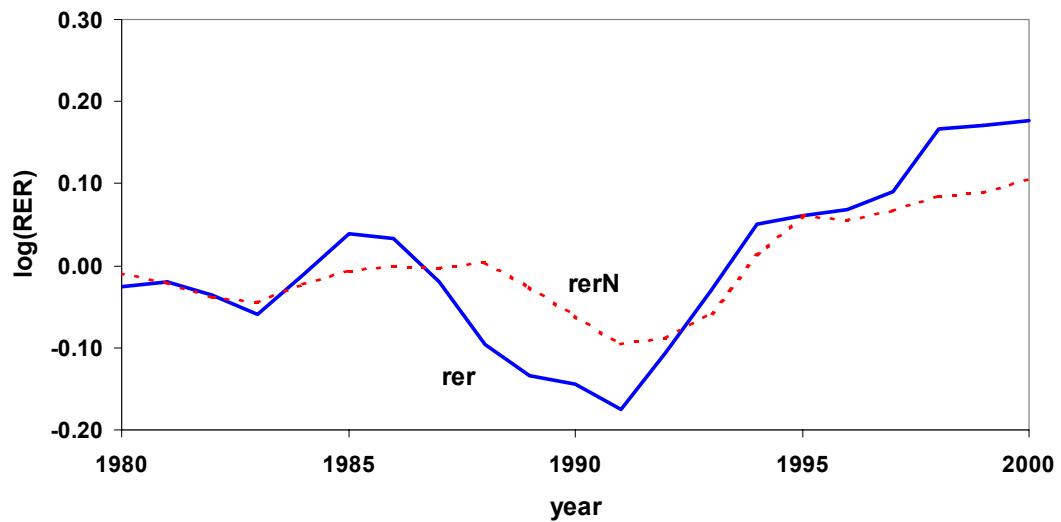


TABLE 2A

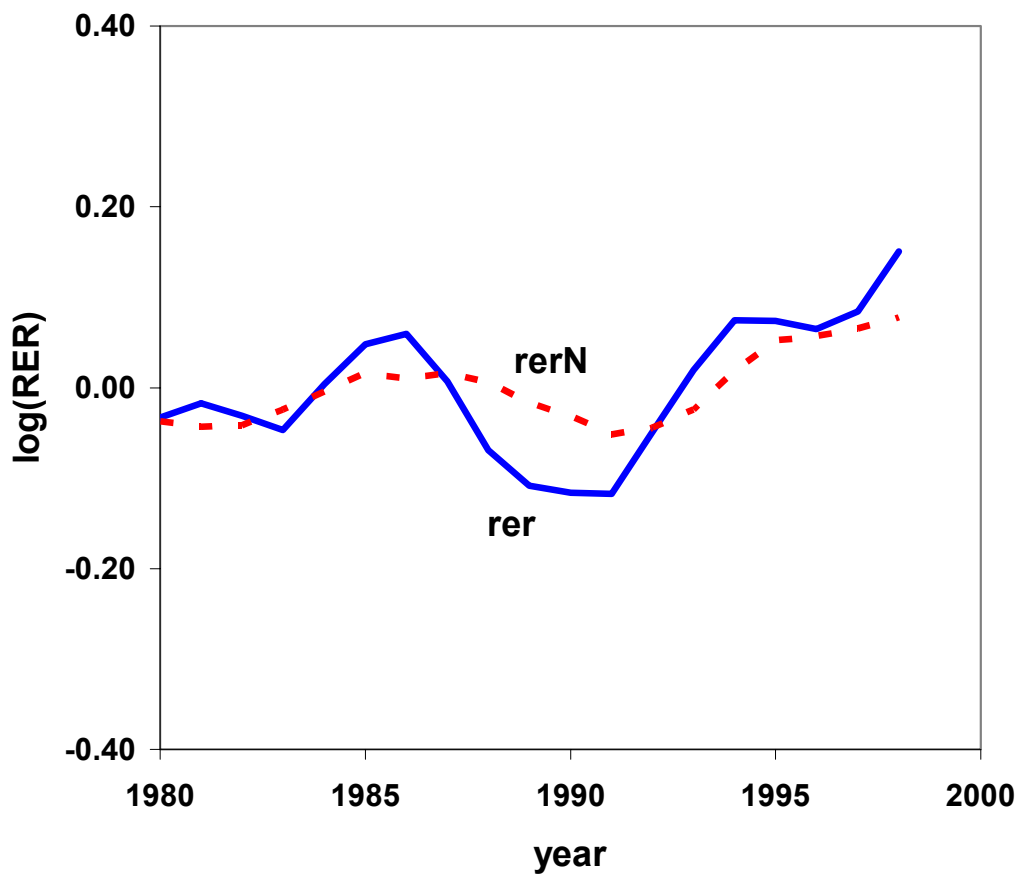
**CANADA-U.S. REAL EXCHANGE RATE**  
**Annual Data**

	GO Deflators 1980-1998	PPI-CPI 1980-2000	Components of CPI 1980-2000	Components of PCD 1980-2000
Levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.81	0.88	0.46	0.42
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.51	0.70	0.63	0.57
<b>vardec(rer,rer<sup>N</sup>)</b>	0.38	0.66	0.33	0.27
Detrended levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.78	0.88	-0.43	-0.32
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.45	0.51	0.17	0.14
<b>vardec(rer,rer<sup>N</sup>)</b>	0.29	0.41	0.02	0.02
1 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.54	0.70	-0.07	-0.11
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.40	0.55	0.20	0.13
<b>vardec(rer,rer<sup>N</sup>)</b>	0.20	0.40	0.09	0.06
4 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.74	0.82	-0.19	-0.08
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.47	0.55	0.16	0.13
<b>vardec(rer,rer<sup>N</sup>)</b>	0.33	0.51	0.12	0.09



**FIGURE 3A**  
**CANADA-U.S. REAL EXCHANGE RATE**

**GO deflators**



**CPI / CPI components**

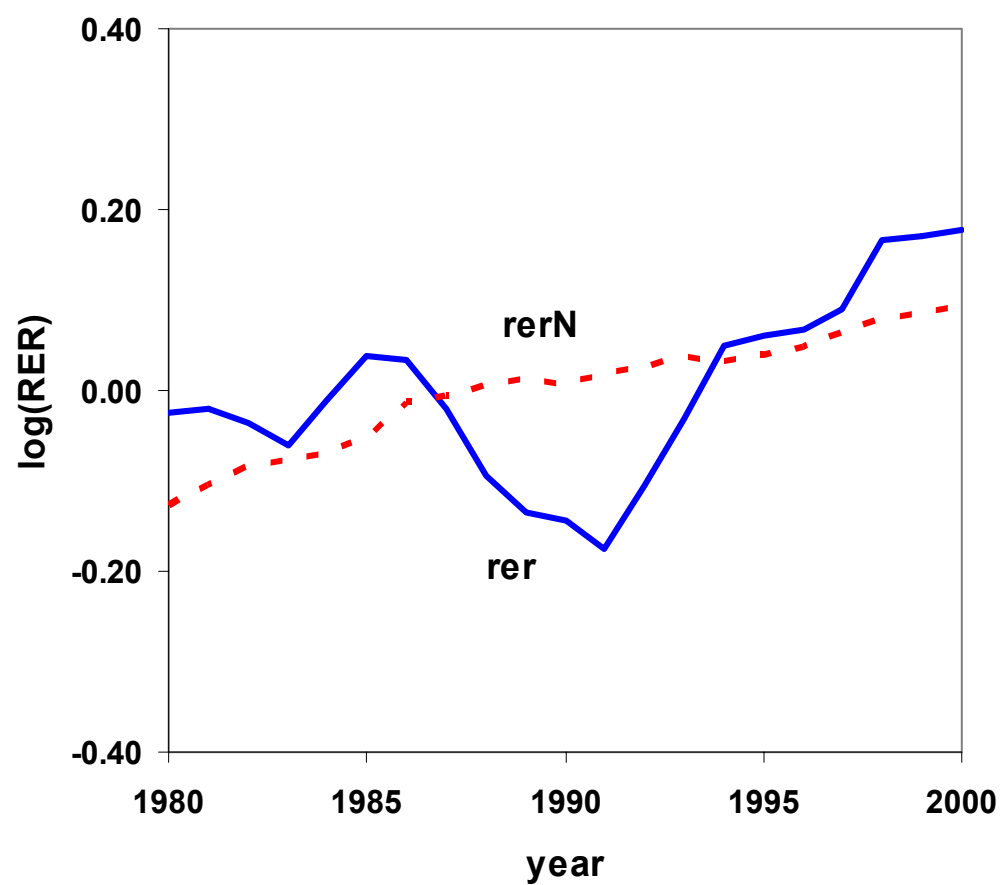


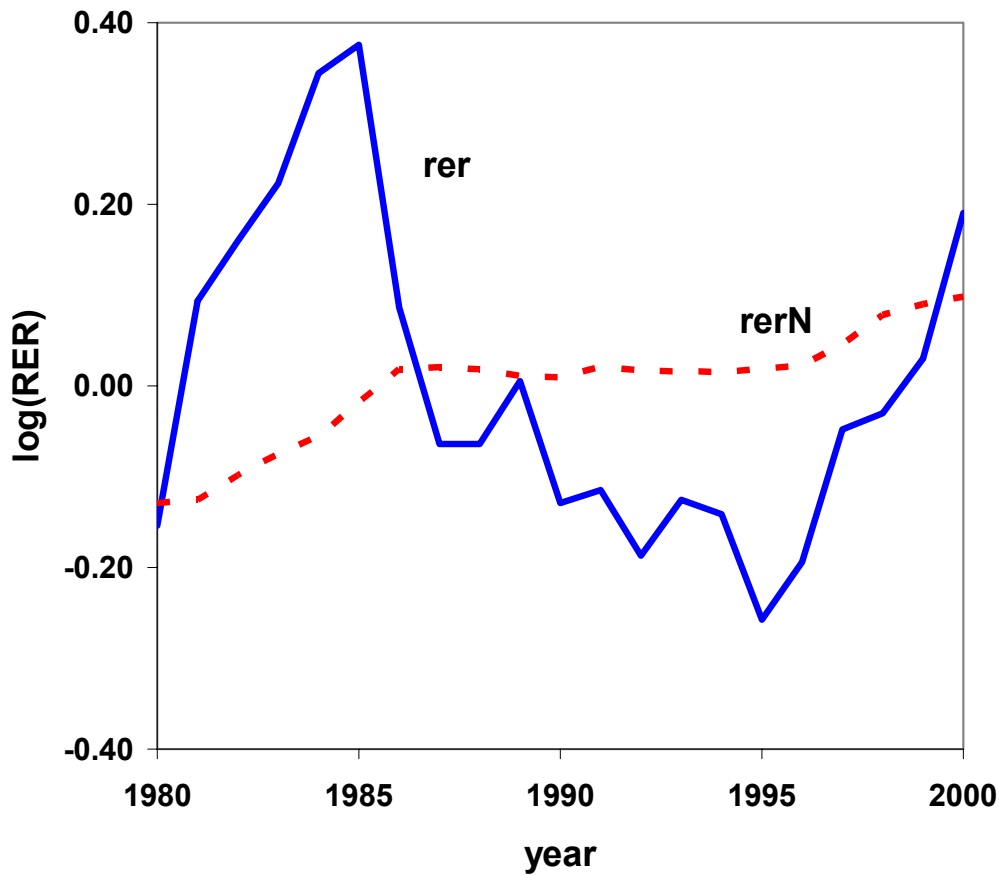
TABLE 2B

**GERMANY-U.S. REAL EXCHANGE RATE****Annual Data**

	GO Deflators 1980-2000	PPI-CPI 1980-2000	Components of CPI 1980-2000	Components of PCD 1980-2000
Levels				
<b>corr(rer,rer<sup>N</sup>)</b>	-0.55	-0.33	-0.05	-0.24
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.25	0.73	0.15	0.25
<b>vardec(rer,rer<sup>N</sup>)</b>	0.04	0.21	0.02	0.05
Detrended levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.18	-0.15	0.24	0.37
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.20	0.13	0.12	0.10
<b>vardec(rer,rer<sup>N</sup>)</b>	0.04	0.02	0.01	0.01
1 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.16	-0.24	0.18	-0.02
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.13	0.14	0.10	0.07
<b>vardec(rer,rer<sup>N</sup>)</b>	0.03	0.04	0.01	0.01
4 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.24	0.02	0.31	0.49
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.21	0.12	0.10	0.09
<b>vardec(rer,rer<sup>N</sup>)</b>	0.07	0.10	0.01	0.02

**FIGURE 3B**  
**GERMANY-U.S. REAL EXCHANGE RATE**

**GO deflators**



**CPI / CPI components**

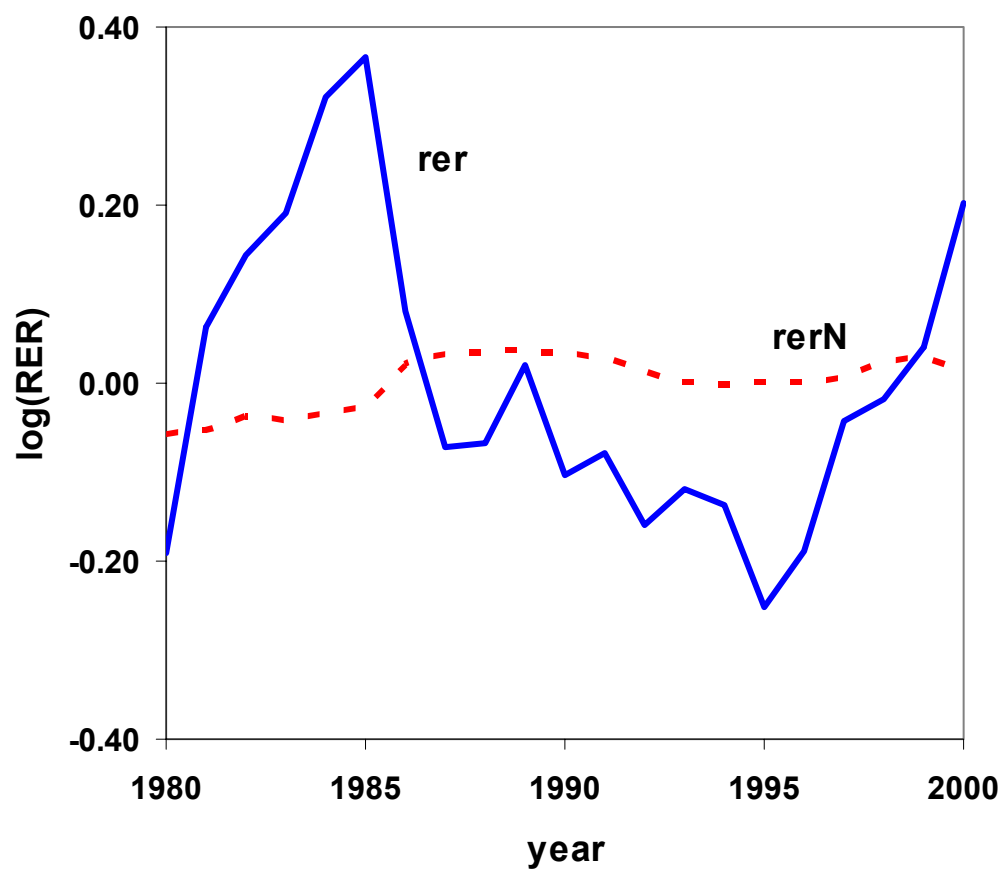


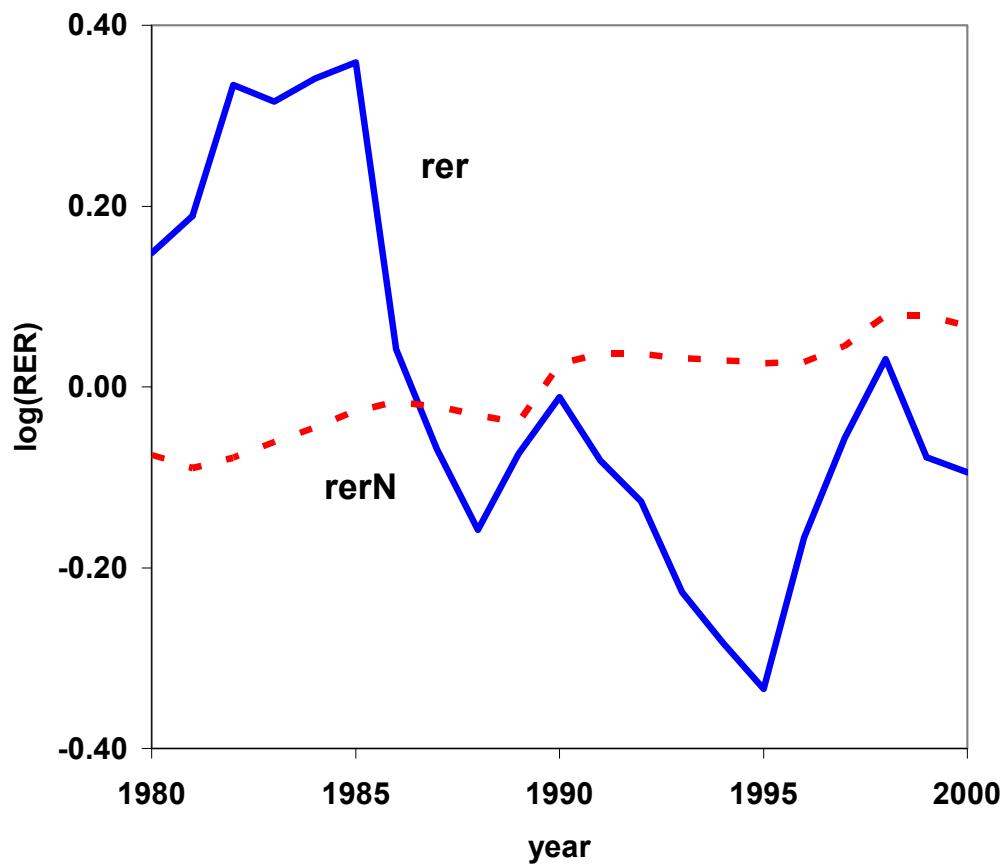
TABLE 2C

**JAPAN-U.S. REAL EXCHANGE RATE**  
**Annual Data**

	GO Deflators 1980-2000	PPI-CPI 1980-2000	Components of CPI 1980-2000	Components of PCD 1990-2000
Levels				
$\text{corr}(\text{rer}, \text{rer}^N)$	-0.33	0.92	-0.74	-0.60
$\text{std}(\text{rer}^N) / \text{std}(\text{rer})$	0.14	0.27	0.17	0.13
$\text{vardec}(\text{rer}, \text{rer}^N)$	0.02	0.11	0.02	0.01
Detrended levels				
$\text{corr}(\text{rer}, \text{rer}^N)$	0.47	0.95	-0.27	0.35
$\text{std}(\text{rer}^N) / \text{std}(\text{rer})$	0.12	0.16	0.07	0.07
$\text{vardec}(\text{rer}, \text{rer}^N)$	0.02	0.03	0.00	0.00
1 year changes				
$\text{corr}(\text{rer}, \text{rer}^N)$	0.30	0.87	-0.32	0.13
$\text{std}(\text{rer}^N) / \text{std}(\text{rer})$	0.12	0.17	0.09	0.07
$\text{vardec}(\text{rer}, \text{rer}^N)$	0.02	0.05	0.01	0.01
4 year changes				
$\text{corr}(\text{rer}, \text{rer}^N)$	0.52	0.95	-0.36	0.43
$\text{std}(\text{rer}^N) / \text{std}(\text{rer})$	0.12	0.16	0.06	0.07
$\text{vardec}(\text{rer}, \text{rer}^N)$	0.02	0.05	0.01	0.01

**FIGURE 3C**  
**JAPAN-U.S. REAL EXCHANGE RATE**

**GO deflators**



**CPI / CPI components**

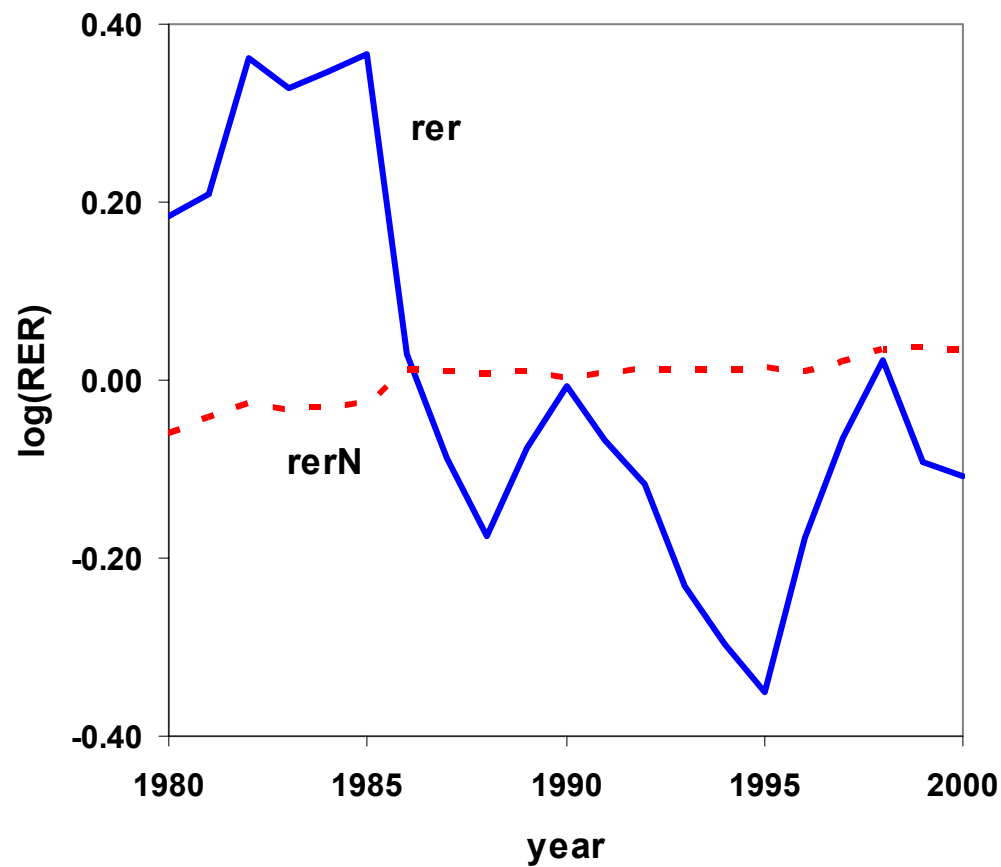


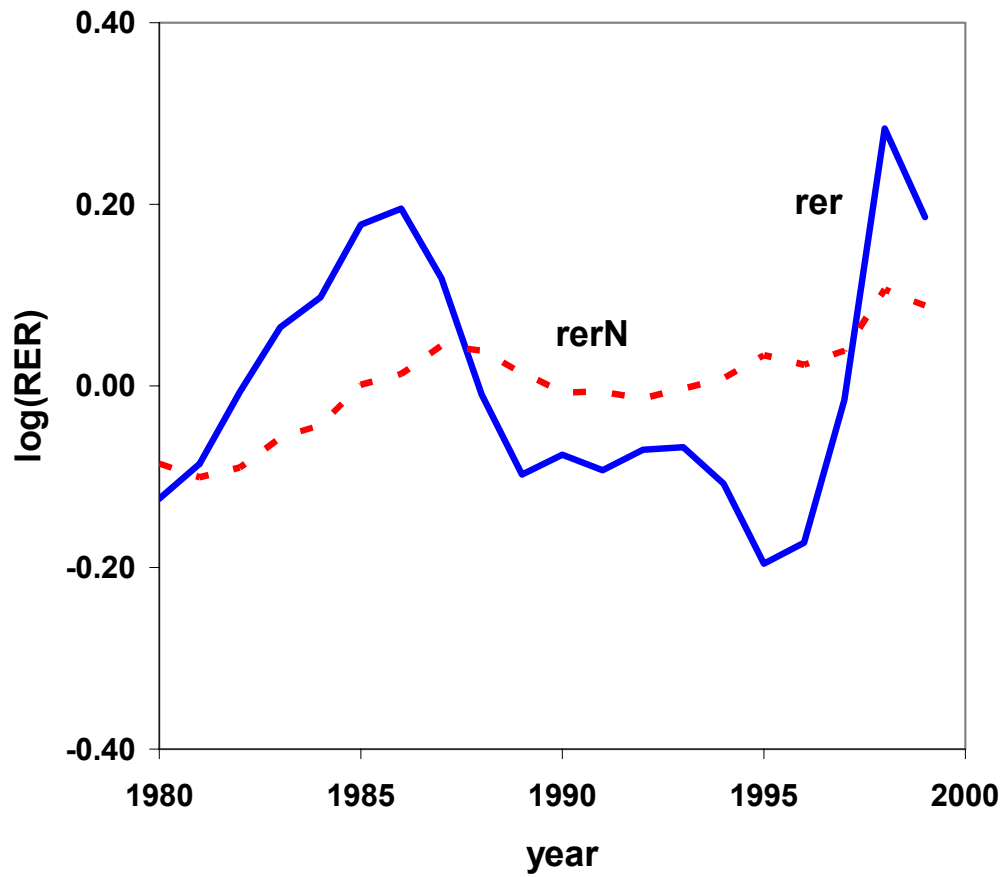
TABLE 2D

**KOREA-U.S. REAL EXCHANGE RATE****Annual Data**

	GO Deflators 1980-2000	PPI-CPI 1980-2000	Components of CPI 1980-2000	Components of PCD 1980-2000
Levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.65	0.43	0.64	0.72
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.21	0.48	0.23	0.36
<b>vardec(rer,rer<sup>N</sup>)</b>	0.05	0.22	0.06	0.18
Detrended levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.82	0.94	0.63	0.72
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.18	0.30	0.21	0.24
<b>vardec(rer,rer<sup>N</sup>)</b>	0.04	0.14	0.05	0.08
1 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.81	0.88	0.57	0.49
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.23	0.26	0.22	0.16
<b>vardec(rer,rer<sup>N</sup>)</b>	0.08	0.10	0.06	0.03
4 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.80	0.94	0.62	0.72
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.18	0.30	0.21	0.24
<b>vardec(rer,rer<sup>N</sup>)</b>	0.05	0.13	0.06	0.08

**FIGURE 3D**  
**KOREA-U.S. REAL EXCHANGE RATE**

**GO deflators**



**CPI / CPI components**

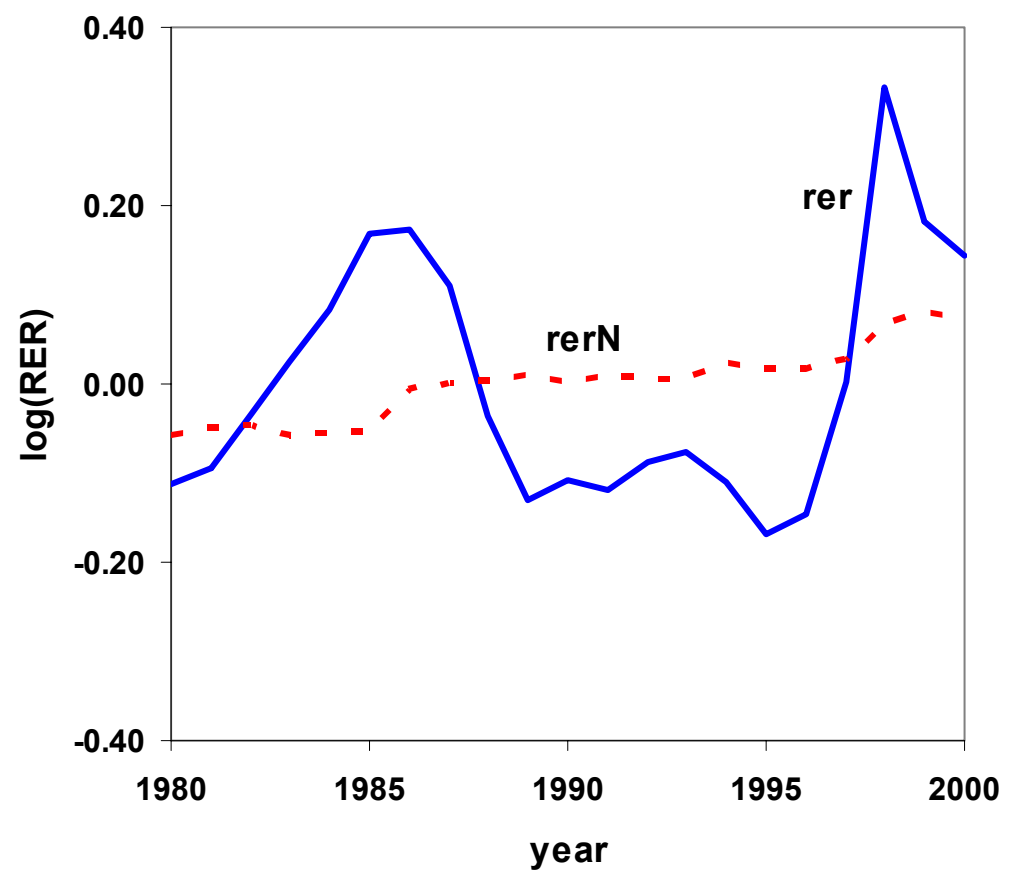


TABLE 2E

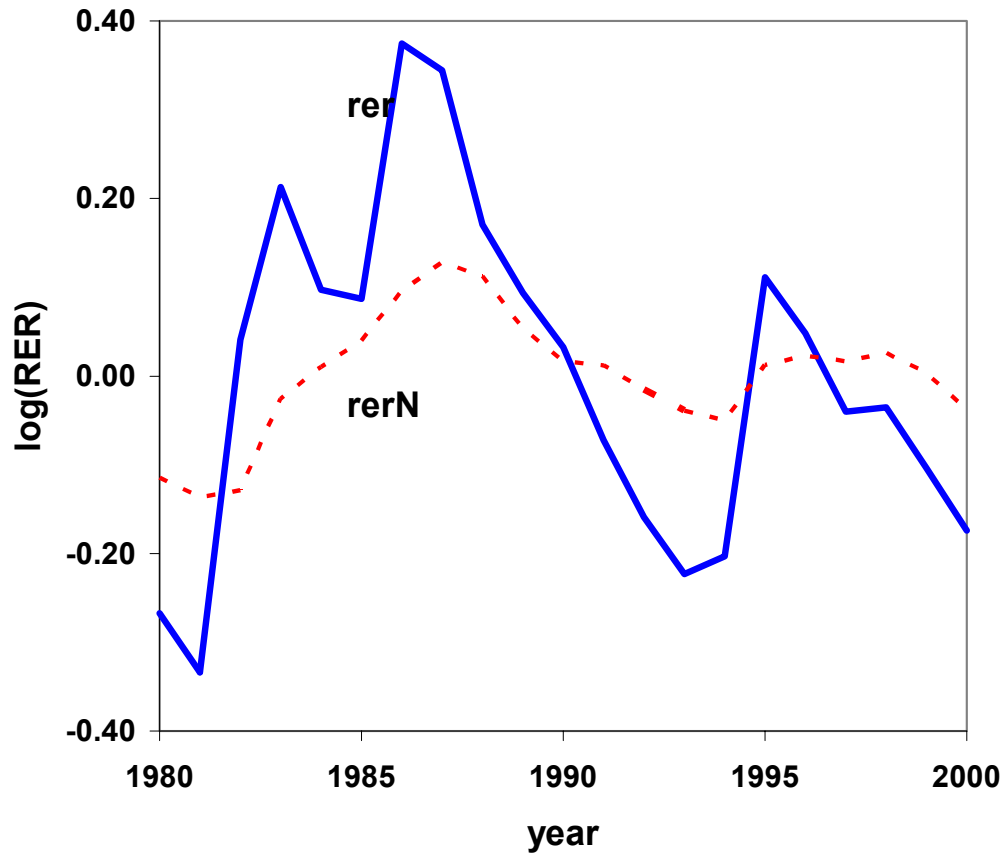
**MEXICO-U.S. REAL EXCHANGE RATE****Annual Data**

	GO Deflators 1980-2000	PPI-CPI 1981-2000	Components of CPI 1980-2000	Components of PCD 1980-2000
Levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.75	0.74	0.64	0.81
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.36	0.21	0.55	0.23
<b>vardec(rer,rer<sup>N</sup>)</b>	0.18	0.06	0.33	0.08
Detrended levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.84	0.73	0.67	0.84
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.36	0.22	0.46	0.24
<b>vardec(rer,rer<sup>N</sup>)</b>	0.20	0.06	0.26	0.08
1 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.52	0.54	0.26	0.51
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.25	0.19	0.28	0.16
<b>vardec(rer,rer<sup>N</sup>)</b>	0.07	0.04	0.08	0.03
4 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.91	0.78	0.73	0.92
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.38	0.24	0.51	0.27
<b>vardec(rer,rer<sup>N</sup>)</b>	0.25	0.08	0.34	0.12



**FIGURE 3E**  
**MEXICO-U.S. REAL EXCHANGE RATE**

**GO deflators**



**CPI / CPI components**

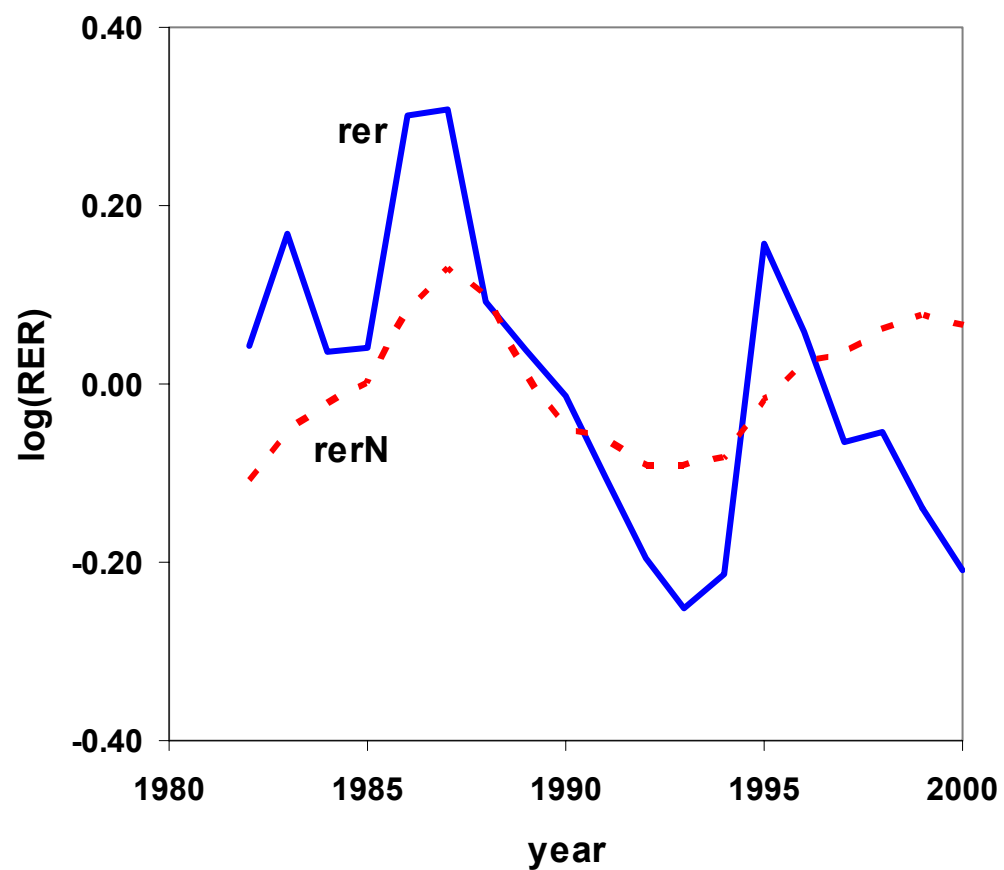


TABLE 3

**COMPARISON OF SERIES:  
TRADE WEIGHTED AVERAGE  
Annual Data**

	GO Deflators	PPI-CPI	Components of CPI	Components of PCD
Levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.44	0.73	0.23	0.27
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.36	0.48	0.45	0.36
<b>vardec(rer,rer<sup>N</sup>)</b>	0.21	0.33	0.22	0.15
Detrended levels				
<b>corr(rer,rer<sup>N</sup>)</b>	0.68	0.77	0.00	0.23
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.32	0.32	0.22	0.15
<b>vardec(rer,rer<sup>N</sup>)</b>	0.18	0.20	0.08	0.03
1 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.47	0.63	0.02	0.14
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.27	0.33	0.19	0.13
<b>vardec(rer,rer<sup>N</sup>)</b>	0.11	0.19	0.06	0.04
4 year changes				
<b>corr(rer,rer<sup>N</sup>)</b>	0.70	0.78	0.10	0.37
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.34	0.34	0.23	0.16
<b>vardec(rer,rer<sup>N</sup>)</b>	0.21	0.25	0.14	0.08

TABLE 4

**COMPARISON OF SERIES:  
CORRELATIONS OF DIFFERENT MEASURES OF  $rer^N$   
Annual Data**

	Canada	Germany	Japan	Korea	Mexico	weighted average
<b>Levels</b>						
PPI-CPI-GO deflator	0.97	0.92	-0.61	0.09	0.70	0.52
CPI components-GO deflator	0.52	0.91	0.85	0.76	0.54	0.64
PCD components-GO deflator	0.54	0.99	0.91	0.02	0.95	0.72
PCD components-CPI components	0.996	0.88	0.94	0.19	0.68	0.84
<b>Detrended levels</b>						
CPI-PPI/GO deflator	0.96	0.54	0.37	0.89	0.71	0.74
CPI components/GO deflator	-0.18	0.83	0.61	0.71	0.82	0.37
PCD components/GO deflator	-0.12	0.88	0.81	0.77	0.96	0.47
PCD components/CPI components	0.92	0.90	0.40	0.88	0.86	0.80
<b>1 year changes</b>						
CPI-PPI/GO deflator	0.88	0.48	0.28	0.88	0.56	0.64
CPI components/GO deflator	-0.19	0.73	0.44	0.52	0.73	0.29
PCD components/GO deflator	-0.14	0.65	0.79	0.59	0.86	0.41
PCD components/CPI components	0.79	0.60	0.48	0.53	0.75	0.69
<b>4 year changes</b>						
CPI-PPI/GO deflator	0.98	0.56	0.47	0.91	0.81	0.80
CPI components/GO deflator	0.04	0.89	0.54	0.69	0.86	0.46
PCD components/GO deflator	0.03	0.97	0.79	0.75	0.97	0.54
PCD components/CPI components	0.87	0.92	0.19	0.91	0.89	0.75

**TABLE 5**  
**COMPARISON OF COUNTRIES: GROSS OUTPUT DEFLATORS**  
**Annual Data**

	Canada	Germany	Japan	Korea	Mexico
Importance of trade to country <i>i</i>					
2000 bilateral trade/GDP	0.58	0.05	0.04	0.14	0.44
2000 bilateral trade/trade	0.82	0.08	0.26	0.20	0.83
Rank of U.S. as partner	1	3	1	1	1
Importance of trade to U.S.					
2000 bilateral trade/U.S. GDP	0.04	0.01	0.02	0.01	0.03
2000 bilateral trade/U.S. trade	0.21	0.04	0.11	0.03	0.13
Rank of country <i>i</i> as partner	1	6	3	7	2
Levels					
<b>corr(rer,rer<sup>N</sup>)</b>	0.81	-0.55	-0.33	0.65	0.75
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.51	0.25	0.14	0.21	0.36
<b>vardec(rer,rer<sup>N</sup>)</b>	0.38	0.04	0.02	0.05	0.18
Detrended levels					
<b>corr(rer,rer<sup>N</sup>)</b>	0.78	0.18	0.47	0.82	0.84
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.45	0.20	0.12	0.18	0.36
<b>vardec(rer,rer<sup>N</sup>)</b>	0.29	0.04	0.02	0.04	0.20
1 year changes					
<b>corr(rer,rer<sup>N</sup>)</b>	0.54	0.16	0.30	0.81	0.52
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.40	0.13	0.12	0.23	0.25
<b>vardec(rer,rer<sup>N</sup>)</b>	0.20	0.03	0.02	0.08	0.07
4 year changes					
<b>corr(rer,rer<sup>N</sup>)</b>	0.74	0.24	0.52	0.80	0.91
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.47	0.21	0.12	0.18	0.38
<b>vardec(rer,rer<sup>N</sup>)</b>	0.33	0.07	0.02	0.05	0.25

TABLE A  
**GROSS DOMESTIC PRODUCT DEFLATORS**  
**Annual Data**

	Canada 1980- 1998	Germany 1980- 2000	Japan 1980- 2000	Korea 1980- 2000	Mexico 1980- 2000	weighted average
Levels						
<b>corr(rer,rer<sup>N</sup>)</b>	0.80	-0.32	-0.69	0.00	0.74	0.34
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.90	0.53	0.22	0.26	0.50	0.59
<b>vardec(rer,rer<sup>N</sup>)</b>	0.69	0.15	0.03	0.06	0.33	0.38
Detrended levels						
<b>corr(rer,rer<sup>N</sup>)</b>	0.63	0.19	-0.24	0.56	0.84	0.47
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.75	0.27	0.18	0.18	0.47	0.49
<b>vardec(rer,rer<sup>N</sup>)</b>	0.48	0.07	0.03	0.04	0.33	0.29
1 year changes						
<b>corr(rer,rer<sup>N</sup>)</b>	0.05	-0.14	-0.29	0.61	0.47	0.11
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.81	0.18	0.16	0.26	0.36	0.48
<b>vardec(rer,rer<sup>N</sup>)</b>	0.33	0.05	0.03	0.09	0.15	0.18
4 year changes						
<b>corr(rer,rer<sup>N</sup>)</b>	0.65	0.18	-0.16	0.56	0.91	0.51
<b>std(rer<sup>N</sup>)/std(rer)</b>	0.68	0.27	0.16	0.19	0.47	0.46
<b>vardec(rer,rer<sup>N</sup>)</b>	0.54	0.12	0.03	0.06	0.40	0.34

TABLE B

**COMPARISON OF GROSS DOMESTIC PRODUCT DEFLATORS  
AND GROSS OUTPUT DEFLATORS**

**Annual Data**

	Canada 1980-1998	Germany 1980-2000	Japan 1980-2000	Korea 1980-2000	Mexico 1980-2000	weighted average
Levels						
<b>corr(rer(GDP),rer(GO))</b>	0.99	0.99	0.997	0.94	0.98	0.99
<b>corr(rer<sup>N</sup>(GDP),rer<sup>N</sup>(GO))</b>	0.96	0.97	0.89	0.86	0.97	0.94
<b>std(rer(GDP))/std(rer(GO))</b>	1.27	1.11	1.10	1.34	1.09	1.18
<b>std(rer<sup>N</sup>(GDP))/std(rer<sup>N</sup>(GO))</b>	2.23	1.68	1.74	1.66	1.52	1.87
Detrended levels						
<b>corr(rer(GDP),rer(GO))</b>	0.98	0.88	0.995	0.99	0.99	0.98
<b>corr(rer<sup>N</sup>(GDP),rer<sup>N</sup>(GO))</b>	0.88	0.80	0.69	0.86	0.98	0.86
<b>std(rer(GDP))/std(rer(GO))</b>	1.07	0.94	1.06	1.22	1.11	1.08
<b>std(rer<sup>N</sup>(GDP))/std(rer<sup>N</sup>(GO))</b>	1.77	1.51	1.57	1.22	1.45	1.59
1 year changes						
<b>corr(rer(GDP),rer(GO))</b>	0.99	0.99	0.99	0.99	0.99	0.99
<b>corr(rer<sup>N</sup>(GDP),rer<sup>N</sup>(GO))</b>	0.87	0.48	0.57	0.76	0.92	0.78
<b>std(rer(GDP))/std(rer(GO))</b>	1.04	1.05	1.05	1.19	1.09	1.06
<b>std(rer<sup>N</sup>(GDP))/std(rer<sup>N</sup>(GO))</b>	2.13	1.50	1.49	1.35	1.58	1.76
4 year changes						
<b>corr(rer(GDP),rer(GO))</b>	0.99	0.998	0.997	0.99	0.99	0.99
<b>corr(rer<sup>N</sup>(GDP),rer<sup>N</sup>(GO))</b>	0.96	0.85	0.71	0.90	0.99	0.91
<b>std(rer(GDP))/std(rer(GO))</b>	1.01	1.07	1.06	1.20	1.14	1.07
<b>std(rer<sup>N</sup>(GDP))/std(rer<sup>N</sup>(GO))</b>	1.47	1.75	1.49	1.28	1.42	1.47

## **EXTENDED RESULTS**

Examine sample of 50 countries and all possible 1225 bilateral real exchange rates.

Use same methodology and summary statistics and CPI-PPI measures of prices.

Examine robustness of results to

1. Presence of U.S. in bilateral trade partner pairs in the sample.
2. Presence of rich-country/poor-country bilateral trade pairs in the sample.
3. Presence of high-inflation/low inflation bilateral trade pairs in the sample.

Find that there is a substantive relation between  $rer_{i,us}$  and  $rer_{i,us}^N$  on average.

The relation does not depend on these three factors (at least in the manner one might expect).

Strength of the relation depends crucially on size of the trade relationship between two trade partners.



## COUNTRIES IN THE SAMPLE

### Average percent world trade 1980–2005

Argentina	0.36	Hong Kong (P.R.C.)	2.52	Peru	0.12
Australia	1.12	India	0.66	Philippines	0.43
Austria	1.14	Indonesia	0.75	Saudi Arabia	1.31
Belgium	2.75	Ireland	0.73	South Africa	1.73
Brazil	0.94	Israel	0.41	Singapore	0.47
Canada	3.67	Italy	4.19	Spain	1.88
Chile	0.25	Japan	6.87	Sri Lanka	0.08
Colombia	0.20	Jordan	0.08	Sweden	1.37
Costa Rica	0.07	Korea	1.95	Switzerland	1.68
Cyprus	0.06	Luxembourg	0.17	Thailand	0.80
Denmark	0.83	Malaysia	1.04	Trinidad and Tobago	0.07
Egypt	0.26	Mexico	1.49	Turkey	0.54
El Salvador	0.04	Netherlands	3.84	United Kingdom	5.19
Finland	0.67	New Zealand	0.25	United States	13.60
France	5.64	Norway	0.79	Uruguay	0.05
Germany	9.24	Pakistan	0.20	Venezuela	0.42
Greece	0.39	Panama	0.15	Total	83.47

## US BILATERAL REAL EXCHANGE RATES

### Means weighted by trade

	all	income level		inflation		trade intensity		std(rer)	
		high	low	high	low	high	low	high	low
<b>levels</b>									
corr(rer, rer <sup>N</sup> )	0.60	0.58	0.69	0.63	0.59	0.72	0.34	0.58	0.63
std(rer <sup>N</sup> )/std(rer)	0.46	0.48	0.41	0.41	0.47	0.52	0.33	0.32	0.64
vdec(rer, rer <sup>N</sup> )	0.30	0.31	0.24	0.22	0.31	0.37	0.12	0.15	0.48
<b>4-quarter differences</b>									
corr(rer, rer <sup>N</sup> )	0.60	0.61	0.56	0.57	0.60	0.68	0.42	0.56	0.64
std(rer <sup>N</sup> )/std(rer)	0.41	0.41	0.39	0.37	0.42	0.47	0.27	0.27	0.58
msedec(rer, rer <sup>N</sup> )	0.20	0.21	0.17	0.17	0.21	0.26	0.08	0.10	0.34
<b>16-quarter differences</b>									
corr(rer, rer <sup>N</sup> )	0.73	0.75	0.66	0.71	0.74	0.82	0.55	0.70	0.78
std(rer <sup>N</sup> )/std(rer)	0.39	0.39	0.39	0.37	0.39	0.45	0.26	0.26	0.55
msedec(rer, rer <sup>N</sup> )	0.24	0.24	0.22	0.22	0.24	0.31	0.09	0.11	0.40
<b>countries</b>	49	27	22	17	32	20	29	34	15
<b>percent US trade</b>	87.2	68.3	18.9	16.0	71.2	59.9	27.3	48.5	38.7

**INCOME LEVELS**  
**ALL BILATERAL REAL EXCHANGE RATES**  
**Means weighted by trade**

	<b>all</b>	<b>high/ high</b>	<b>high/ low</b>	<b>low/ low</b>
<b>levels</b>				
corr( $rer$ , $rer^N$ )	0.52	0.46	0.72	0.63
std( $rer^N$ )/std( $rer$ )	0.64	0.67	0.49	0.55
vdec( $rer$ , $rer^N$ )	0.33	0.33	0.32	0.33
<b>4-quarter differences</b>				
corr( $rer$ , $rer^N$ )	0.51	0.50	0.57	0.61
std( $rer^N$ )/std( $rer$ )	0.50	0.53	0.39	0.43
msedec( $rer$ , $rer^N$ )	0.22	0.22	0.18	0.22
<b>16-quarter differences</b>				
corr( $rer$ , $rer^N$ )	0.64	0.63	0.66	0.71
std( $rer^N$ )/std( $rer$ )	0.51	0.54	0.41	0.45
msedec( $rer$ , $rer^N$ )	0.28	0.28	0.26	0.30
<b>bilateral pairs</b>	1225	378	616	231
<b>percent of world trade</b>	71.0	56.0	14.0	1.0

**INFLATION LEVELS**  
**ALL BILATERAL REAL EXCHANGE RATES**  
**Means weighted by trade**

	<b>all</b>	<b>high/ high</b>	<b>high/ low</b>	<b>low/ low</b>
<b>levels</b>				
corr( $rer$ , $rer^N$ )	0.52	0.66	0.66	0.49
std( $rer^N$ )/std( $rer$ )	0.64	0.54	0.48	0.67
vdec( $rer$ , $rer^N$ )	0.33	0.32	0.28	0.34
<b>4-quarter differences</b>				
corr( $rer$ , $rer^N$ )	0.51	0.66	0.58	0.50
std( $rer^N$ )/std( $rer$ )	0.50	0.41	0.36	0.53
mseedec( $rer$ , $rer^N$ )	0.22	0.23	0.17	0.22
<b>16-quarter differences</b>				
corr( $rer$ , $rer^N$ )	0.64	0.78	0.69	0.63
std( $rer^N$ )/std( $rer$ )	0.51	0.42	0.38	0.53
mseedec( $rer$ , $rer^N$ )	0.28	0.28	0.24	0.28
<b>bilateral pairs</b>	1225	136	561	528
<b>percent of world trade</b>	71.0	0.6	10.5	59.8

# TRADE INTENSITY AND REAL EXCHANGE RATE VARIABILITY

## ALL BILATERAL REAL EXCHANGE RATES

Means weighted by trade

	all	trade intensity		std(rer)	
		high	low	high	low
<b>levels</b>					
corr(rer, rer <sup>N</sup> )	0.52	0.57	0.47	0.63	0.44
std(rer <sup>N</sup> )/std(rer)	0.64	0.71	0.57	0.42	0.79
vdec(rer, rer <sup>N</sup> )	0.33	0.37	0.29	0.24	0.39
<b>4-quarter differences</b>					
corr(rer, rer <sup>N</sup> )	0.51	0.57	0.47	0.58	0.47
std(rer <sup>N</sup> )/std(rer)	0.50	0.64	0.38	0.32	0.63
msedec(rer, rer <sup>N</sup> )	0.22	0.28	0.16	0.13	0.27
<b>16-quarter differences</b>					
corr(rer, rer <sup>N</sup> )	0.64	0.69	0.60	0.69	0.60
std(rer <sup>N</sup> )/std(rer)	0.51	0.61	0.43	0.33	0.64
msedec(rer, rer <sup>N</sup> )	0.28	0.33	0.23	0.18	0.34
<b>bilateral pairs</b>	1225	49	1176	918	307
<b>percent world trade</b>	71.0	32.0	38.9	29.6	41.4

## CHINA BILATERAL REAL EXCHANGE RATES

Means weighted by trade  
Annual data

	all	income level		inflation		trade intensity		std(rer)	
		high	low	high	low	high	low	high	low
<b>levels</b>									
corr(rer, rer <sup>N</sup> )	0.79	0.80	0.71	0.79	0.79	0.84	0.74	0.78	0.81
std(rer <sup>N</sup> )/std(rer)	0.65	0.67	0.48	0.54	0.66	0.81	0.48	0.45	0.88
vdec(rer, rer <sup>N</sup> )	0.46	0.47	0.34	0.41	0.46	0.59	0.32	0.30	0.64
<b>1-year lags</b>									
corr(rer, rer <sup>N</sup> )	0.38	0.37	0.46	0.57	0.37	0.44	0.30	0.42	0.32
std(rer <sup>N</sup> )/std(rer)	0.38	0.38	0.35	0.36	0.38	0.44	0.31	0.27	0.49
msecdec(rer, rer <sup>N</sup> )	0.16	0.16	0.15	0.17	0.16	0.21	0.11	0.09	0.24
<b>4-year lags</b>									
corr(rer, rer <sup>N</sup> )	0.86	0.87	0.76	0.86	0.86	0.92	0.79	0.84	0.88
std(rer <sup>N</sup> )/std(rer)	0.56	0.57	0.44	0.48	0.56	0.63	0.48	0.41	0.73
msecdec(rer, rer <sup>N</sup> )	0.48	0.49	0.33	0.39	0.48	0.60	0.35	0.29	0.69
<b>countries</b>	50	28	22	17	33	2	48	40	10
<b>percent China trade</b>	89.4	82.3	7.1	3.9	85.5	47.0	42.4	47.2	42.2

**TRADE BLOCS**  
**US BILATERAL REAL EXCHANGE RATES**  
Means weighted by trade

	<b>all</b>	<b>EU</b>	<b>non-EU</b>	<b>NAFTA</b>	<b>non-NAFTA</b>	<b>other</b>
<b>levels</b>						
corr( $rer$ , $rer^N$ )	0.60	0.27	0.71	0.81	0.52	0.63
std( $rer^N$ )/std( $rer$ )	0.46	0.32	0.51	0.55	0.42	0.48
vdec( $rer$ , $rer^N$ )	0.30	0.10	0.36	0.49	0.20	0.26
<b>4-quarter differences</b>						
corr( $rer$ , $rer^N$ )	0.60	0.41	0.66	0.69	0.55	0.63
std( $rer^N$ )/std( $rer$ )	0.41	0.22	0.47	0.50	0.37	0.45
msedec( $rer$ , $rer^N$ )	0.20	0.05	0.25	0.33	0.14	0.19
<b>16-quarter differences</b>						
corr( $rer$ , $rer^N$ )	0.73	0.57	0.79	0.80	0.70	0.78
std( $rer^N$ )/std( $rer$ )	0.39	0.22	0.44	0.49	0.34	0.41
msedec( $rer$ , $rer^N$ )	0.24	0.07	0.29	0.39	0.17	0.22
<b>countries</b>	49	14	35	2	47	33
<b>percent US trade</b>	87.2	21.0	66.2	28.6	58.6	37.6

**TRADE BLOCS**  
**ALL BILATERAL REAL EXCHANGE RATES**  
Means weighted by trade

	<b>all</b>	<b>EU/ EU</b>	<b>EU/ NAFTA</b>	<b>EU/ other</b>	<b>NAFTA/ NAFTA</b>	<b>NAFTA/ other</b>	<b>other/ other</b>
<b>levels</b>							
corr( $rer$ , $rer^N$ )	0.52	0.35	0.30	0.54	0.81	0.63	0.67
std( $rer^N$ )/std( $rer$ )	0.64	0.88	0.33	0.59	0.54	0.49	0.57
vdec( $rer$ , $rer^N$ )	0.33	0.35	0.11	0.32	0.48	0.27	0.38
<b>4-quarter differences</b>							
corr( $rer$ , $rer^N$ )	0.51	0.43	0.41	0.44	0.69	0.63	0.60
std( $rer^N$ )/std( $rer$ )	0.50	0.71	0.22	0.37	0.50	0.44	0.42
msedec( $rer$ , $rer^N$ )	0.22	0.27	0.06	0.15	0.33	0.19	0.21
<b>16-quarter differences</b>							
corr( $rer$ , $rer^N$ )	0.64	0.57	0.55	0.56	0.80	0.78	0.69
std( $rer^N$ )/std( $rer$ )	0.51	0.72	0.24	0.43	0.49	0.41	0.44
msedec( $rer$ , $rer^N$ )	0.28	0.33	0.08	0.23	0.38	0.23	0.31
<b>bilateral pairs</b>	1225	91	42	462	3	99	528
<b>percent world trade</b>	71.0	23.1	6.6	12.3	7.9	11.3	9.8



## ALL BILATERAL REAL EXCHANGE RATES

### Unweighted means

	all	trade intensity		std(rer)		trading blocs					
		high	low	high	low	EU/ EU	EU/ NAFTA	EU/ other	NAFTA/ NAFTA	NAFTA/ other	other/ other
<b>levels</b>											
corr(rer, rer <sup>N</sup> )	0.59	0.56	0.60	0.66	0.39	0.52	0.50	0.56	0.74	0.60	0.65
std(rer <sup>N</sup> )/std(rer)	0.59	0.87	0.58	0.53	0.77	0.85	0.34	0.54	0.42	0.53	0.63
vdec(rer, rer <sup>N</sup> )	0.35	0.40	0.35	0.34	0.36	0.41	0.14	0.30	0.30	0.30	0.40
<b>4-quarter differences</b>											
corr(rer, rer <sup>N</sup> )	0.51	0.52	0.51	0.55	0.39	0.47	0.51	0.49	0.59	0.54	0.53
std(rer <sup>N</sup> )/std(rer)	0.43	0.72	0.42	0.38	0.58	0.70	0.24	0.37	0.40	0.46	0.45
msedec(rer, rer <sup>N</sup> )	0.20	0.27	0.20	0.18	0.24	0.28	0.07	0.16	0.22	0.20	0.23
<b>16-quarter differences</b>											
corr(rer, rer <sup>N</sup> )	0.59	0.62	0.59	0.62	0.48	0.60	0.57	0.56	0.65	0.63	0.60
std(rer <sup>N</sup> )/std(rer)	0.46	0.70	0.45	0.42	0.60	0.70	0.26	0.40	0.39	0.47	0.49
msedec(rer, rer <sup>N</sup> )	0.28	0.35	0.28	0.27	0.31	0.36	0.09	0.23	0.24	0.27	0.33
<b>bilateral pairs</b>	1225	49	1176	918	307	91	42	462	3	99	528
<b>percent world trade</b>	71.0	32.0	38.9	29.6	41.4	23.1	6.6	12.3	7.9	11.3	9.8

## TRADE WEIGHTED REGRESSIONS

Standard errors in parentheses

	sum income	diff income	sum inflation	diff inflation	trade intensity	std(rer)	EU/ EU	EU/ NAFTA	EU/ other	NAFTA/ NAFTA	NAFTA/ other	constant	$R^2$
<b>levels</b>													
corr(rer, rer <sup>N</sup> )	-0.004 (0.018)	-0.011 (0.021)	-0.200 (0.131)	0.044 (0.151)	0.314* (0.117)	1.617* (0.165)	-0.099* (0.037)	-0.268* (0.044)	-0.024 (0.037)	0.091 (0.080)	-0.013 (0.037)	0.382 (0.380)	0.292
std(rer <sup>N</sup> )/std(rer)	-0.019 (0.020)	0.064* (0.023)	0.066 (0.142)	0.392* (0.163)	0.821* (0.127)	-2.813* (0.179)	-0.001 (0.040)	-0.236* (0.047)	-0.0414 (0.040)	-0.714* (0.087)	-0.197* (0.040)	1.336* (0.412)	0.363
vdec(rer, rer <sup>N</sup> )	-0.015 (0.011)	0.011 (0.013)	-0.048 (0.080)	0.202* (0.092)	0.230* (0.071)	-0.878* (0.101)	-0.121* (0.022)	-0.264* (0.027)	-0.074* (0.022)	-0.088 (0.049)	-0.144* (0.022)	0.821* (0.232)	0.242
<b>4-quarter lags</b>													
corr(rer, rer <sup>N</sup> )	0.001 (0.009)	-0.070* (0.011)	-0.116 (0.067)	0.035 (0.077)	0.003 (0.060)	1.520* (0.085)	-0.029 (0.019)	-0.173* (0.022)	-0.098* (0.019)	0.181* (0.041)	0.058* (0.019)	0.352 (0.195)	0.419
std(rer <sup>N</sup> )/std(rer)	-0.011 (0.021)	0.099* (0.024)	0.072 (0.148)	0.100 (0.170)	1.016* (0.132)	-2.631* (0.186)	0.012 (0.041)	-0.169* (0.049)	-0.084* (0.041)	-0.712* (0.090)	-0.096* (0.041)	0.951* (0.428)	0.313
mseedec(rer, rer <sup>N</sup> )	-0.008 (0.008)	0.021* (0.009)	0.035 (0.054)	0.058 (0.062)	0.235* (0.048)	-0.965* (0.068)	-0.048* (0.015)	-0.155* (0.018)	-0.081* (0.015)	-0.088* (0.033)	-0.050* (0.015)	0.519* (0.157)	0.354
<b>16-quarter lags</b>													
corr(rer, rer <sup>N</sup> )	-0.007 (0.011)	-0.092* (0.013)	-0.173* (0.076)	0.246* (0.088)	0.218* (0.068)	1.358* (0.096)	-0.018 (0.021)	-0.129* (0.026)	-0.071* (0.021)	0.041 (0.047)	0.080* (0.021)	0.616* (0.221)	0.333
std(rer <sup>N</sup> )/std(rer)	-0.011 (0.019)	0.098* (0.023)	0.104 (0.139)	0.060 (0.159)	0.406* (0.123)	-2.524* (0.175)	0.033 (0.039)	-0.198* (0.046)	-0.080* (0.039)	-0.351* (0.085)	-0.097* (0.039)	1.014* (0.402)	0.301
mseedec(rer, rer <sup>N</sup> )	-0.016 (0.009)	0.026* (0.011)	-0.034 (0.067)	0.229* (0.077)	0.297* (0.060)	-1.111* (0.085)	-0.076* (0.019)	-0.208* (0.022)	-0.090* (0.019)	-0.159* (0.041)	-0.110* (0.019)	0.778* (0.195)	0.314

## **THEORETICAL MODEL**

Take new approach to investigating origins of real exchange rate fluctuations — allow goods to differ by degree of tradability.

Two factors determine tradability of a good:

1. degree of substitutability in consumption with same good produced in other countries
2. size of real cost of trade between any two countries for a particular good.

**IN THE MODEL, THE DEGREE OF TRADABILITY OF A GOOD IS EXACTLY EQUAL TO ITS DEGREE OF ACTUAL TRADEDNESS.**

# OUTLINE

## 1. MOTIVATION

Characterize sources of real exchange rate movements; changes in international relative prices of nontraded/traded goods.

## 2. THEORY

Develop  $J$  sector,  $I$  country intertemporal model of real exchange rate determination.

Allow three possible sources of deviations from law of one price at sectoral level.

## 3. CALIBRATED MODEL

Quantitatively evaluate a 3 sector, 2 country model, calibrated to data on Mexico and United States.

## 4. MODEL WITH MONEY

Superimpose a quantity theory model of money to be able to compare nominal and real exchange rate movements.

**FUNDAMENTAL HYPOTHESIS IS THAT TRADABILITY  
EQUALS TRADEDNESS.**

# MOTIVATION

$$RER = NER \times \frac{P_{us}}{P_{mex}}$$

$$= \frac{\textit{pesos}}{\textit{dollar}} \times \frac{\textit{dollars/basket}_{us}}{\textit{pesos/basket}_{mex}} = \frac{\textit{baskets}_{mex}}{\textit{basket}_{us}}$$

Traditional way to think about RER movements:

no movements in international relative price of traded goods when law of one price holds.

movements in internal relative price of nontraded to traded goods across countries determines RER.

Suppose law of one price holds for all traded goods;

$$P_{mex}^T = NER \times P_{us}^T.$$

RER when law of one price holds is

$$RER^N = \frac{P_{mex}^T}{P_{us}^T} \times \frac{P_{us}}{P_{mex}},$$

$$RER^N = \frac{P_{us}}{P_{us}^T} / \frac{P_{mex}}{P_{mex}^T}.$$

$RER^N$  is exactly equal to the RER when there are no law of one price deviations.

Compare  $RER$  and  $RER^N$  in data for Mexico and US 1980-1998; they are not the same at all.

$$\sigma(RER) = 2.81 \times \sigma(RER^N),$$

$$\text{corr}(RER, RER^N) = 0.82.$$

Traded goods: agriculture, mining, and manufacturing;

Nontraded goods: services and construction.



**TABLE 1****Tradedness and Deviations From Law of One Price:  
1980-1998**

<b>Sector</b>	<b>Tradedness</b>	<b>Deviation</b>
<b>Primarys *</b>	20.37	17.63
<b>Manufactures *</b>	36.37	15.10
<b>Services</b>	4.30	24.26

**Tradedness**

$$100 \times (\text{imports}_{i,1993} + \text{exports}_{i,1993}) / \text{gross output}_{i,1993}$$

**Deviation**

$$100 \times \left[ \sum_{t=1980}^{1998} (\log RER_{it} - \overline{\log RER_i})^2 / 18 \right]^{1/2},$$

where  $RER_{it}$  is real exchange rate for sector  $i$

( $RER_{it}$  is constant if law of one price holds).

# THE MODEL

There are  $I$  countries,  $J$  sectors/types of goods in every country.

Same types of good produced in different countries are imperfect substitutes in consumption.

In addition, goods are technologically differentiated: there are transactions costs of trade.

Size of costs of trade plus degree of substitutability in consumption determine tradability of each of  $I \times J$  goods.

# CONSUMER-WORKERS

Representative consumer in country  $i$  has the period utility function:

$$u^i(c_1^i(c_{11}^i, \dots, c_{1I}^i), \dots, c_J^i(c_{J1}^i, \dots, c_{JI}^i), \ell^i; z^i)$$

Here,  $c_{jh}^i$  is consumption in country  $i$  of good  $j$  produced in country  $h$ ,  $\ell^i$  is leisure in country  $i$ , and  $z^i$  is a real demand shock.

# SECTORS

Each good is produced by one sector with a production function of the form (for country  $h$ , good  $j$ )

$$y_{jh} = f_{jh}(\ell_{jh}).$$

Economy must satisfy the feasibility conditions

$$\sum_{i=1}^I (1 + \delta_{jh}^i) c_{jh}^i = y_{jh}, \quad j = 1, \dots, J; \quad h = 1, \dots, I;$$

$$\sum_{j=1}^J \ell_{ji} + \ell^i = \bar{\ell}^i, \quad i = 1, \dots, I.$$

# UNCERTAINTY

At every date  $t$ , there are  $K$  possible events  $\eta_t = 1, \dots, K$ ;  $(z^1(\eta_t), \dots, z^I(\eta_t))$  are idiosyncratic demand shocks at  $t$ .

$\eta$  is governed by a stationary first order Markov process, with transition matrix  $\Pi(\eta, \eta')$  where  $\pi_{ij} = \text{prob}(\eta_t = j | \eta_{t-1} = i)$ .

A *state* is a history of events  $s = (\eta_0, \eta_1, \dots, \eta_{t(s)})$ ;

then  $\pi(s) = \pi_{\eta_0\eta_1} \pi_{\eta_1\eta_2} \cdots \pi_{\eta_{t(s)-1}\eta_{t(s)}}$ .

Set of states  $S$  is countable.

# THE CONSUMER'S SEQUENTIAL MARKETS PROBLEM

Consumers can trade in spot markets and a complete set of Arrow securities in every state.

$$\max \sum_{s \in S} \beta^{t(s)} \pi(s) u^i(c_{1s}^i, \dots, c_{Js}^i, \ell_s^i; z^i(\eta_s))$$

$$s.t. \sum_{j=1}^J \sum_{h=1}^I (1 + \delta_{jh}^i) p_{jhs} c_{jhs}^i + \sum_{\eta'=1}^K q_{(s,\eta')} b_{(s,\eta')}^i$$

$$\leq w_s^i (\bar{\ell}^i - \ell_s^i) + r_s^i + b_s^i \text{ for all } s$$

$$c_{js}^i = c_j^i(c_{j1s}^i, \dots, c_{jIs}^i) \text{ for all } i, j, s$$

$$r_s^i = \sum_{j=1}^J (p_{jis} y_{jis} - w_s^i \ell_{jis}^i) \text{ for all } i, s$$

$$b_s^i \geq -\bar{B} \text{ for all } s$$

$$b_{\eta_0}^i = 0.$$

# PROFIT MAXIMIZATION BY SECTORS

$$\max p_{jhs} y_{jhs} - w_s^h \ell_{jhs}$$

$$s. t. \quad y_{jhs} = f_{jh}(\ell_{jhs}).$$

$$r_s^i = \sum_{j=1}^J (p_{jis} y_{jis} - w_s^i \ell_{jis})$$

# SEQUENTIAL MARKETS EQUILIBRIUM

A *sequential markets equilibrium* is a sequence of quantities  $(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{\ell}_s^i, \hat{b}_s^i, \hat{y}_{jhs}, \hat{\ell}_{jhs})$ , prices  $(\hat{p}_{jhs}^i, \hat{w}_s^i, \hat{q}_{(s,\eta)})$ , and profits  $\hat{r}_s^i$ , such that

i) given prices and profits the quantities  $(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{\ell}_s^i, \hat{b}_s^i)$  solve the utility maximization problem of consumer  $i$ ;

ii) given prices, the quantities  $(\hat{y}_{jhs}, \hat{\ell}_{jhs})$  solve the profit maximization problem of sector  $j$  in country  $h$  in state  $s$ ;

iii)  $\hat{r}_s^i$  are profits in country  $i$  in state  $s$ ;

iv) the quantities  $(\hat{c}_{jhs}^i, \hat{\ell}_s^i, \hat{y}_{jhs}, \hat{\ell}_{jhs})$  satisfy the feasibility conditions;

v) the Arrow securities  $\hat{b}_s^i$  satisfy the market clearing conditions

$$\sum_{i=1}^I \hat{b}_s^i = 0 \text{ in state } s.$$



# COMPUTING EQUILIBRIUM

## WORLD PLANNER'S DYNAMIC PROBLEM

For a given vector of welfare weights  $a = (a^1, \dots, a^I)$  solve the world planner's problem

$$\max \sum_{i=1}^I a^i \sum_{s \in S} \beta^{t(s)} \pi(s) u^i(c_{1s}^i, \dots, c_{ns}^i, \ell_s^i; z^i(\eta_s))$$

$$s.t. \sum_{i=1}^I (1 + \delta_{jh}^i) c_{jhs}^i \leq f_{jh}(\ell_{jhs}) \text{ for all } j, h, s$$

$$\sum_{j=1}^J \ell_{jis} + \ell_s^i \leq \bar{\ell}^i \text{ for all } i, s$$

$$c_{js}^i = c_j^i(c_{j1s}^i, \dots, c_{jIs}^i) \text{ for all } i, j, s.$$

# WORLD PLANNER'S STATIC PROBLEM

It is easy to show that the solution to this infinite horizon problem can be derived by solving the  $K$  static problems

$$\max \sum_{i=1}^I a^i u^i(c_1^i, \dots, c_J^i, \ell^i; z^i(\eta))$$

$$s. t. \sum_{i=1}^I (1 + \delta_{jh}^i) c_{jh}^i \leq f_{jh}(\ell_{jh}) \text{ for all } j, h$$

$$\sum_{j=1}^J \ell_{jh} + \ell^i \leq \bar{\ell}^i \text{ for all } i$$

$$c_j^i = c_j^i(c_{j1}^i, \dots, c_{jI}^i) \text{ for all } i, j.$$

Denote the solution to this problem by

$$(c_j^i(a, \eta), c_{jh}^i(a, \eta), \ell^i(a, \eta), y_{jh}(a, \eta), \ell_{jh}(a, \eta)).$$

# PRICES

Define the prices  $(p_{jh}(a, \eta), w^i(a, \eta), q(a, \eta, \eta'))$  and profits  $P^h(a, \eta)$  by the following rules

$$p_{jh}(a, \eta) = a^h \frac{\partial u^h(c_1^h, \dots, c_n^h, \ell^h; z^h(\eta))}{\partial c_j^h} \\ \times \frac{\partial c_j^h(c_{j1}^h, \dots, c_{jm}^h)}{\partial c_{jh}^h}$$

$$w^i(a, \eta) = a^i \frac{\partial u^i(c_1^i, \dots, c_n^i, \ell^i; z^i(\eta))}{\partial \ell^i}$$

$$q(a, \eta, \eta') = \beta \pi_{\eta, \eta'}.$$

$$r^h(a, \eta) = \sum_{j=1}^J (p_{jh}(a, \eta) y_{jh}(a, \eta) - w^h(a, \eta) \ell_{jh}(a, \eta)).$$

Numeraire is marginal social welfare in event  $\eta$ .

# TRANSFER FUNCTIONS

The transfer to country  $i$  when event  $\eta$  occurs is given by

$$\tau^i(a, \eta) = \sum_{j=1}^J \sum_{h=1}^I p_{jh}(a, \eta)(1 + \delta_{jh}^i)c_{jh}^i(a, \eta) - \sum_{j=1}^J p_{ji}(a, \eta)y_{ji}(a, \eta).$$

$\tau^i(a, \eta)$  is the trade deficit of country  $i$  when event  $\eta$  occurs (measured in units of marginal social welfare in event  $\eta$ ).

The present value of all current and future savings given utility weights  $a$  and current event  $\eta$  is given by

$$b^i(a, \eta) = -\tau^i(a, \eta) + \beta \sum_{\eta'=1}^K \pi_{\eta\eta'} b^i(a, \eta').$$

Notice that this is a Bellman equation.

# Theorem 1

Suppose that sequence of quantities  $\left( \hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{\ell}_s^i, \hat{b}_s^i, \hat{y}_{jhs}, \hat{\ell}_{jhs} \right)$ , prices  $\left( \hat{p}_{jhs}^i, \hat{w}_s^i, \hat{q}_{(s,\eta)} \right)$ , and profits  $\hat{r}_s^i$  is an equilibrium. Then  $\left( \hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{\ell}_s^i, \hat{b}_s^i, \hat{y}_{jhs}, \hat{\ell}_{jhs} \right)$  solves the static social planner's problem in event  $\eta_s$ .

Conversely suppose that  $(c_j^i(\hat{a}, \eta), c_{jh}^i(\hat{a}, \eta), \ell^i(\hat{a}, \eta), y_{jh}(\hat{a}, \eta), \ell_{jh}(\hat{a}, \eta))$  solves the static social planner's problem. If  $b^i(\hat{a}, \eta_0) = 0$  for all  $i$ , then the sequence

$$\left( \hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{\ell}_s^i, \hat{b}_s^i, \hat{y}_{jhs}, \hat{\ell}_{jhs} \right) = (c_j^i(\hat{a}, \eta_s), c_{jh}^i(\hat{a}, \eta_s), \ell^i(\hat{a}, \eta_s), y_{jh}(\hat{a}, \eta_s), \ell_{jh}(\hat{a}, \eta_s))$$

$\left( \hat{p}_{jhs}^i, \hat{w}_s^i, \hat{q}_{(s,\eta)} \right) = (p_{jh}(\hat{a}, \eta_s), w^i(\hat{a}, \eta_s), q(\hat{a}, \eta_s, \eta))$ , and  $\hat{r}_s^i = r^i(\hat{a}, \eta_s)$  is an equilibrium.

## Theorem 2

There exists a vector of welfare weights,  $\hat{a} = (\hat{a}^1, \dots, \hat{a}^I)$  such that  $b^i(\hat{a}, \eta_0) = 0$ ,  $i = 1, \dots, I$ .

In practice, rather than compute  $\hat{a}$ , we calibrate the model so that the values of output, consumption, and trade in a benchmark year, 1993 in the case of our Mexico-U.S. model, are an equilibrium. This allows us to calibrate the vector  $\hat{a}$

# CALIBRATED MODEL

Calibrate sectoral parameters  $(\zeta_j^i, \theta_{jh}, \delta_{jh}^i)$  to match bilateral trade and output numbers by sector for benchmark year, 1993.

Take elasticity parameters from international real business cycle literature.

Compute statistics from 1980-1998 data that is logged and linearly detrended.

Compare statistics to those implied by model.

Markov process for  $\eta_t$  is calibrated, matches standard deviations/ autocorrelations of output.

Compare deviations from the law of one price with those in the model, sector by sector.

# MEXICO-US CALIBRATED MODEL

$$u^i(c_{pri}^i, c_{man}^i, c_{ser}^i, \ell^i; z^i) = \frac{\left( z^i \left( \left( \sum_{j=pri,man,ser} \zeta_j^i c_j^{i\gamma} \right)^{1/\gamma} \right)^\epsilon + (1 - z^i) \ell^{i\epsilon} \right)^{\psi/\epsilon} - 1}{\psi},$$

where

$$c_j^i = (\alpha_{mex} c_{j,mex}^{i\rho} + \alpha_{us} c_{j,us}^{i\rho})^{\frac{1}{\rho}}, \quad j = pri, man, ser$$

$$y_{ji} = \theta_{ji} \ell_{ji}^{\lambda_{ji}}, \quad j = pri, man, ser; \quad i = mex, us$$

$$c_{j,mex}^{mex} + c_{j,mex}^{us} (1 + \delta_{j,mex}^{us}) = y_{j,mex}, \quad j = pri, man, ser$$

$$c_{j,us}^{mex} (1 + \delta_{j,us}^{mex}) + c_{j,us}^{us} = y_{j,us}, \quad j = pri, man, ser.$$



**TABLE 2****1993 Benchmark Data Set  
(Billion U.S. Dollars)**

<b>Variable</b>	<b>Mexico</b>	<b>U. S.</b>
$y_{pri}^j$	42.528	393.037
$y_{man}^j$	200.469	3082.868
$y_{ser}^j$	391.132	7820.442
$(1 + \delta_{pri,j}^{mex})c_{pri,j}^{mex}$	35.870	2.006
$(1 + \delta_{pri,j}^{us})c_{pri,j}^{us}$	6.658	391.031
$(1 + \delta_{man,j}^{mex})c_{man,j}^{mex}$	167.197	39.629
$(1 + \delta_{man,j}^{us})c_{man,j}^{us}$	33.272	3043.239
$(1 + \delta_{ser,j}^{mex})c_{ser,j}^{mex}$	382.778	8.451
$(1 + \delta_{ser,j}^{us})c_{ser,j}^{us}$	8.354	7811.991

## PARAMETERIZE MARKOV PROCESS

Grid of 3 shocks on  $(\bar{z}^i - 1/d^i, \bar{z}^i, \bar{z}^i + d^i)$ .

$$\Pi^i = \begin{bmatrix} 1 - 2\pi^i & \pi^i & \pi^i \\ \pi^i & 1 - 2\pi^i & \pi^i \\ \pi^i & \pi^i & 1 - 2\pi^i \end{bmatrix}$$

3 parameters  $(\bar{z}^i, d^i, \pi^i)$  to match 3 observations for each country:

- 1993 output compared to mean output
- standard deviation of output
- serial correlation of output.

Shocks are independent across countries.  $K = 3 \times 3$ .

# CALIBRATION OF TRANSPORTATION COSTS

$$\frac{\partial u^{mex}}{\partial c_{man}^{mex}} (\alpha_{mex} c_{man,mex}^{mex\rho} + \alpha_{us} c_{man,us}^{mex\rho})^{\frac{1}{\rho}-1} \alpha_{mex} c_{man,mex}^{mex\rho-1} = p_{man,mex}$$

$$\frac{\partial u^{mex}}{\partial c_{man}^{mex}} (\alpha_{mex} c_{man,mex}^{mex\rho} + \alpha_{us} c_{man,us}^{mex\rho})^{\frac{1}{\rho}-1} \alpha_{us} c_{man,us}^{mex\rho-1} = p_{man,us} (1 + \delta_{man,us}^{mex})$$

$$\frac{c_{man,us}^{mex}}{c_{man,mex}^{mex}} = \left( \frac{\alpha_{us} p_{man,mex}}{\alpha_{mex} p_{man,us} (1 + \delta_{man,us}^{mex})} \right)^{\frac{1}{1-\rho}}$$

In base year, 1993,  $p_{man,mex} = p_{man,us} = 1$ ,

$$\frac{(1 + \delta_{man,us}^{mex}) c_{man,us}^{mex}}{c_{man,mex}^{mex}} = \left( \frac{\alpha_{us}}{\alpha_{mex}} \right)^{\frac{1}{1-\rho}} (1 + \delta_{man,us}^{mex})^{\frac{-\rho}{1-\rho}}.$$

Similarly,

$$\frac{c_{man,us}^{us}}{(1 + \delta_{man,mex}^{us}) c_{man,mex}^{us}} = \left( \frac{\alpha_{us}}{\alpha_{mex}} \right)^{\frac{1}{1-\rho}} (1 + \delta_{man,mex}^{us})^{\frac{\rho}{1-\rho}}.$$

In the absence of  $\delta_{jh}^i$ 's,

$$\frac{c_{man,us}^{mex}}{c_{man,mex}^{mex}} = \frac{c_{man,us}^{us}}{c_{man,mex}^{us}} = \frac{y_{man,us}}{y_{man,mex}} = \frac{3082.868}{200.469} = 15.378$$

Suppose  $\rho = 0.8$ ,  $\alpha_{mex} = 0.4$ ,  $\alpha_{us} = 0.6$ :

$$\frac{(1 + \delta_{man,us}^{mex})c_{man,us}^{mex}}{c_{man,mex}^{mex}} = \frac{33.272}{167.197} = 0.199, \quad \delta_{man,us}^{mex} = 1.485$$

$$\frac{c_{man,us}^{us}}{(1 + \delta_{man,mex}^{us})c_{man,mex}^{us}} = \frac{3043.239}{39.629} = 76.793, \quad \delta_{man,mex}^{us} = 0.783.$$

Notice that  $\rho = 0.8$  implies far more substitutability than does  $\rho = 0.33$ . With  $\rho = 0.33$  (and  $\alpha_{mex} = 0.25$ ,  $\alpha_{us} = 0.75$ ),

$$\delta_{man,us}^{mex} = 739.232, \quad \delta_{man,mex}^{us} = 239.964.$$

Home country bias is large for low values of  $\rho$ .

We have much lower values of  $\delta_{jh}^i$  if we allow  $\alpha_{jh}^i$  to differ across countries. (The models are equivalent.)

**TABLE 3****Parameter Values**

parameter	value	source
$\gamma$	-1.25	Stockman/Tesar (1994)
$\epsilon$	0.00	Backus/Kehoe/Kydland (1992)
$\rho$	0.33	Backus/Kehoe/Kydland (1994)
$\psi$	-1.00	Backus/Kehoe/Kydland (1992)
$\lambda_{ji}$	0.33	Chari/Kehoe/McGrattan (1997)

# MOMENTS

Consider some variable  $x$  in country  $i$  and a second variable  $y$  in country  $h$ ;  $i, h = mex, us$  :  $x^i(\eta^1, \eta^2)$  and  $y^h(\eta^1, \eta^2)$ .

**Mean of  $x^i$ :**

$$\mu(x^i) = \sum_{\eta^1=1}^3 \sum_{\eta^2=1}^3 \bar{\pi}_{\eta^1}^1 \bar{\pi}_{\eta^2}^2 x^i(\eta^1, \eta^2)$$

**Variance of  $x^i$ :**

$$\sigma^2(x^i) = \sum_{\eta^1=1}^3 \sum_{\eta^2=1}^3 \bar{\pi}_{\eta^1}^1 \bar{\pi}_{\eta^2}^2 (x^i(\eta^1, \eta^2) - \mu(x^i))^2$$

## Correlation of $x^i$ and $y^h$ :

$$\begin{aligned}\rho(x^i, y^h) &= \frac{1}{\sigma(x^i)\sigma(y^h)} \\ &\times \sum_{\eta^1=1}^3 \sum_{\eta^2=1}^3 \bar{\pi}_{\eta^1}^1 \bar{\pi}_{\eta^2}^2 (x^i(\eta^1, \eta^2) - \mu(x^i)) \\ &\times (y^h(\eta^1, \eta^2) - \mu(y^h))\end{aligned}$$

## Autocorrelation of $x^i$ :

$$\begin{aligned}\rho(x^i, x^{i'}) &= \frac{1}{\sigma^2(x^i)} \\ &\times \sum_{\eta^1=1}^{K^1} \sum_{\eta^2=1}^{K^2} \bar{\pi}_{\eta^1}^1 \bar{\pi}_{\eta^2}^2 (x^i(\eta^1, \eta^2) - \mu(x^i)) \\ &\times \sum_{\eta^{1'}=1}^3 \sum_{\eta^{2'}=1}^3 \pi_{\eta^1 \eta^{1'}} \pi_{\eta^2 \eta^{2'}} (x^i(\eta^{1'}, \eta^{2'}) - \mu(x^i))\end{aligned}$$

Here,  $\bar{\pi}_{\eta^i}^i$  is invariant distribution of  $\eta^i$ .

# RESULTS

## TABLE 4

### Deviations from Law of One Price

	DATA	MODEL
<b>Primaryes</b>	17.69	13.45
<b>Manufactures</b>	15.10	12.03
<b>Services</b>	24.18	18.94

### Deviation

$$100 \times \left\{ \sum_{\eta^1=1}^3 \sum_{\eta^2=1}^3 \bar{\pi}_{\eta^1}^1 \bar{\pi}_{\eta^2}^2 [\log(p_{j1}(\eta^1, \eta^2)/p_{j2}(\eta^1, \eta^2)) - \mu(\log(p_{j1}/p_{j2}))]^2 \right\}^{1/2}$$



**TABLE 5****Standard Deviations and Autocorrelations**

	<b>DATA</b>		<b>MODEL</b>	
	$\sigma$	$\rho$	$\sigma$	$\rho$
<b>Y<sup>us</sup></b>	2.417	0.506	2.417	0.506
<b>TB<sup>us</sup></b>	0.060	0.616	0.107	0.563
<b>Y<sup>mex</sup></b>	4.950	0.578	4.950	0.578
<b>TB<sup>mex</sup></b>	1.448	0.599	2.467	0.563
<b>RER</b>	19.519	0.586	16.276	0.564
<b><math>\widehat{\text{RER}}</math></b>	6.949	0.807	4.008	0.565

**TABLE 6****Correlations  
data/(model)**

	<b>Y<sup>us</sup></b>	<b>TB<sup>us</sup></b>	<b>Y<sup>mex</sup></b>	<b>TB<sup>mex</sup></b>	<b>RER</b>
<b>TB<sup>us</sup></b>	-0.284 (-0.421)				
<b>Y<sup>mex</sup></b>	-0.209 (0.071)	0.286 (0.866)			
<b>TB<sup>mex</sup></b>	0.473 (0.421)	-0.984 (-0.979)	-0.361 (-0.870)		
<b>RER</b>	0.343 (0.426)	-0.736 (-0.996)	-0.747 (-0.870)	0.781 (0.992)	
<b>RER<sup>N</sup></b>	0.322 (0.421)	-0.371 (-0.993)	-0.836 (-0.874)	0.436 (0.996)	0.817 (0.999)

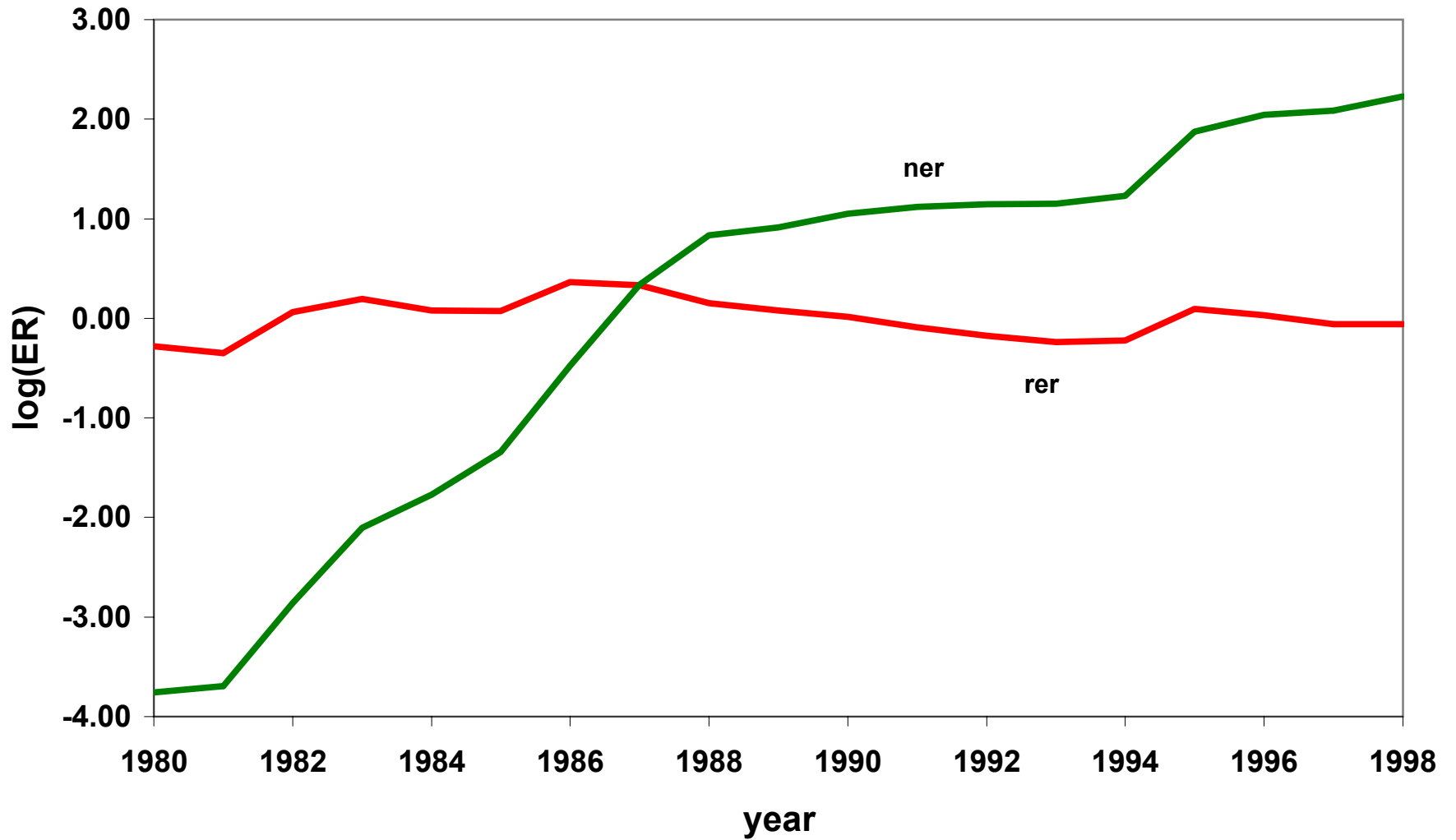
**TABLE 7****Deviations from Law of One Price  
Alternative Specifications**

	<b>DATA</b>	<b>MODEL</b>	<b>MODEL</b>	<b>MODEL</b>	<b>MODEL</b>
		<b>base case</b>	$\rho = 0.80$	$\lambda_{ji} = 0.25$	$\gamma = -4.00$
<b>pri</b>	17.63	13.45	7.72	18.12	12.88
<b>man</b>	15.10	12.03	6.25	16.03	11.06
<b>ser</b>	24.26	18.94	16.10	26.91	19.77

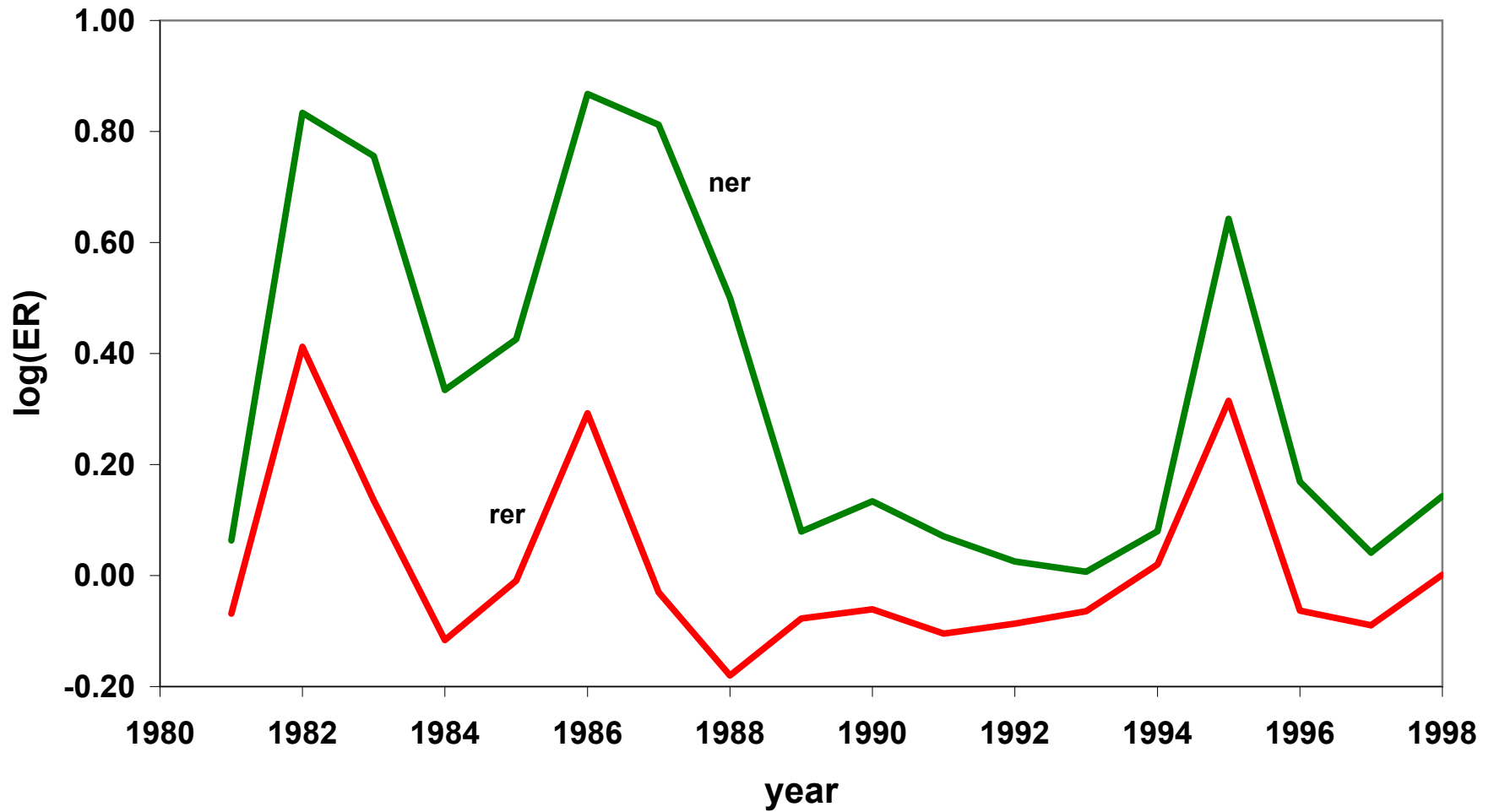
**TABLE 8****Standard Deviations - Alternative Specifications**

	<b>DATA</b>	<b>MODEL</b>	<b>MODEL</b>	<b>MODEL</b>	<b>MODEL</b>
		<b>base case</b>	$\rho = 0.80$	$\lambda_{ji} = 0.25$	$\gamma = -4.00$
<b>Y<sup>us</sup></b>	2.417	2.417	2.417	2.417	2.417
<b>TB<sup>us</sup></b>	0.060	0.107	0.236	0.136	0.098
<b>Y<sup>mex</sup></b>	4.950	4.950	4.950	4.950	4.950
<b>TB<sup>mex</sup></b>	1.448	2.467	5.184	3.390	2.267
<b>RER</b>	19.519	16.276	12.240	22.629	16.385
<b>RER<sup>N</sup></b>	6.949	4.008	5.726	6.250	5.011

# Mexico-U.S. Exchange Rates



# Mexico-U.S. Exchange Rates First Differences



# MONETARY MODEL

Money is a veil.

Each country  $i = 1, 2, \dots, I$  has a monetary authority that prints distinct fiat currency  $i$ .

Goods must be paid for in the currency of the producer's country.

## MONETARY SHOCKS

$$M_{(s,\eta')}^i = \mu^i(\eta')M_s^i.$$

As before,  $\eta$  is governed by a stationary first order Markov process with transition matrix  $\Pi(\eta, \eta')$ .

Consumers are paid interest on money balances. (No monetary friction!)

## BUDGET CONSTRAINTS

$$\sum_{j=1}^J \sum_{h=1}^I (1 + \delta_{jh}^i) E_{hs}^i P_{js}^h c_{jhs}^i + E_{1s}^i \sum_{\eta'=1}^K Q_{(s,\eta')} B_{(s,\eta')}^i + M_s^i \leq W_s^i (\bar{l}^i - l_s^i) + R_s^i + E_{1s}^i B_s^i + \mu^i(\eta) M_{s-1}^i$$

$P_{js}^h$  is the price of good  $j$  produced in country  $h$  in state  $s$  in units of currency  $h$ ,

$E_{hs}^i$  is the nominal exchange rate in units of currency  $i$  per unit of currency  $h$  in state  $s$ ,

$W_s^i$  is the wage in country  $i$  in units of currency  $i$ ,

$B_s^i(s, \eta')$  is purchases in state  $s$  of a security that pays one unit of currency 1 if event  $\eta'$  occurs at  $t(s) + 1$ ,

$Q_{(s,\eta')}$  is the state  $s$  currency 1 price of a unit of currency 1 delivered at  $t(s) + 1$  if  $\eta'$  occurs,

$R_s^i$  are profits in country  $i$  in units of currency  $i$ .



## QUANTITY EQUATION

$$\sum_{j=1}^J \sum_{h=1}^I (1 + \delta_{ji}^h) P_{js}^i c_{jis}^h = M_s^i \text{ for all } s, i.$$

# SEQUENTIAL MARKETS EQUILIBRIUM

A *sequential markets equilibrium* is a sequence of quantities  $(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{l}_s^i, \hat{l}_{jhs}^i, \hat{y}_{jhs}^i, \hat{B}_s^i, \hat{M}_s^i)$ , prices  $(\hat{P}_{js}^i, \hat{W}_s^i, \hat{Q}_s^i, \hat{E}_{hs}^i)$ , and profits  $\hat{R}_s^i$  such that

i) given prices and profits, the quantities  $(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{l}_s^i, \hat{B}_s^i, \hat{M}_s^i)$  solve the utility maximization problem of consumer  $i$ ;

ii) given prices, the quantities  $(\hat{l}_{jhs}^i, \hat{y}_{jhs}^i)$  solve the profit maximization problem of sector  $j$  in country  $h$  in state  $s$ ;

iii) the money stock  $\hat{M}_s^i$  satisfies  $\hat{M}_s^i = \mu^i(\eta)\hat{M}_{s-1}^i$ ;

iv)  $\hat{R}_s^i$  are profits in country  $i$  in state  $s$ ;

v) the quantities  $(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{l}_s^i, \hat{l}_{jhs}^i, \hat{y}_{jhs}^i)$  satisfy the feasibility conditions;

vi) the securities  $\hat{B}_s^i$  satisfy the market clearing conditions

$$\sum_{i=1}^I \hat{B}_s^i = 0 \text{ in state } s.$$

### Theorem 3

Suppose that the sequence of quantities

$(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{l}_s^i, \hat{l}_{jhs}^i, \hat{y}_{jhs}^i, \hat{B}_s^i, \hat{M}_s^i)$ , prices  $(\hat{P}_{js}^i, \hat{W}_s^i, \hat{Q}_s^i, \hat{E}_{hs}^i)$ , and profits  $\hat{R}_s^i$  is an equilibrium of the the monetary economy. Then there exist bond holdings  $\hat{b}_s^i$ , prices  $(\hat{p}_{jhs}^i, \hat{w}_s^i, \hat{q}_s^i)$ , and profits  $\hat{r}_s^i$  that, together with the quantities  $(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{l}_s^i, \hat{l}_{jhs}^i, \hat{y}_{jhs}^i)$  are an equilibrium of the economy without money.

Conversely, suppose that the sequence of quantities

$(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{l}_s^i, \hat{l}_{jhs}^i, \hat{y}_{jhs}^i, \hat{b}_s^i)$ , prices  $(\hat{p}_{jhs}^i, \hat{w}_s^i, \hat{q}_s^i)$ , and profits  $\hat{r}_s^i$  is an equilibrium of the economy without money. Suppose too that  $\mu^i(\eta)$  are monetary shocks and  $\bar{M}_0^i$  are initial values of money. Then there exist bond holdings  $\hat{B}_s^i$ , money stocks  $\hat{M}_s^i$ , prices  $(\hat{P}_{js}^i, \hat{W}_s^i, \hat{Q}_s^i, \hat{E}_{hs}^i)$ , and profits  $\hat{R}_s^i$  that, together with the quantities  $(\hat{c}_{js}^i, \hat{c}_{jhs}^i, \hat{l}_s^i, \hat{l}_{jhs}^i, \hat{y}_{jhs}^i)$  are an equilibrium of the monetary economy.

**TABLE 9****Standard Deviations of First Differences**

	<b>DATA</b>	<b>MODEL</b>
$\Delta Y^{\text{us}}$	2.117	2.402
$\Delta TB^{\text{us}}$	0.051	0.100
$\Delta Y^{\text{mex}}$	4.177	4.548
$\Delta TB^{\text{mex}}$	1.264	2.306
$\Delta RER$	16.560	15.190
$\Delta RER^N$	3.988	3.739
$\Delta M^{\text{us}}$	2.692	2.692
$\Delta P^{\text{us}}$	2.031	3.340
$\Delta M^{\text{mex}}$	15.706	15.706
$\Delta P^{\text{mex}}$	23.675	17.756
$\Delta NER$	31.964	29.082

**TABLE 10****Correlations of First Differences  
data/(model)**

	$\Delta Y^{\text{us}}$	$\Delta \text{TB}^{\text{us}}$	$\Delta Y^{\text{mex}}$	$\Delta \text{TB}^{\text{mex}}$	$\Delta \text{RER}$
$\Delta \text{TB}^{\text{us}}$	0.346 (-0.449)				
$\Delta Y^{\text{mex}}$	0.092 (0.075)	0.651 (0.847)			
$\Delta \text{TB}^{\text{mex}}$	-0.296 (0.449)	-0.958 (-0.970)	-0.730 (-0.849)		
$\Delta \text{RER}$	-0.388 (0.455)	-0.820 (-0.995)	-0.730 (-0.852)	0.856 (0.990)	
$\Delta \text{RER}^N$	0.226 (0.593)	-0.398 (-0.990)	-0.735 (-0.856)	0.518 (0.995)	0.547 (0.999)

**TABLE 11**  
**Additional Correlations of First Differences**  
**data/(model)**

	$\Delta M^{us}$	$\Delta P^{us}$	$\Delta M^{mex}$	$\Delta P^{mex}$	$\Delta NER$
$\Delta Y^{us}$	0.144 (0.144)	-0.346 (-0.603)	-0.244 (0.003)	0.087 (-0.032)	-0.115 (0.288)
$\Delta TB^{us}$	0.130 (-0.066)	-0.052 (0.270)	-0.353 (-0.290)	-0.110 (-0.473)	-0.502 (-0.840)
$\Delta Y^{mex}$	-0.181 (0.009)	0.161 (-0.046)	-0.335 (-0.335)	-0.571 (-0.553)	-0.811 (-0.777)
$\Delta TB^{mex}$	-0.062 (0.066)	0.026 (-0.270)	0.282 (0.291)	0.123 (0.475)	0.532 (0.838)
$\Delta RER$	0.239 (0.067)	-0.119 (-0.274)	0.460 (0.292)	0.233 (0.476)	0.699 (0.845)
$\Delta RER^N$	0.115 (0.066)	-0.226 (-0.271)	0.431 (0.293)	0.593 (0.478)	0.737 (0.845)
$\Delta P^{us}$	-0.477 (0.702)				
$\Delta M^{mex}$	-0.075 (-0.075)	0.247 (-0.056)			
$\Delta P^{mex}$	-0.009 (-0.068)	0.085 (-0.032)	0.637 (0.970)		
$\Delta NER$	0.147 (-0.088)	-0.062 (-0.278)	0.694 (0.751)	0.856 (0.863)	

# CONCLUSIONS

1. The more trade there is between countries, the more important are changes in the relative price of nontraded goods in determining real exchange rate fluctuations.
2. The more traded are the goods of a country with respect to a trade partner, the less important are deviations from the law of one price for real exchange rates.
3. A model that allows goods to be differentiated by degree of tradability (tradedness) does well in accounting for deviations from the law of one price and for RER fluctuations.
4. The same model does a very reasonable job of matching international business cycle facts.