# Productivity, Taxes, and Hours Worked in Spain 1975-2000 

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## Questions:

What has driven economic growth and fluctuations in Spain since 1975? Changes in productivity or changes in factor inputs?

What has been the impact of changes in taxes on aggregate hours worked and on output?

## Framework:

Cole-Ohanian (1999) and Kehoe-Prescott (2002): growth accounting + general equilibrium growth model

Other researchers have stressed the role of labor market institutions: Blanchard and Jimeno (1999), Blanchard and Summers (1986), Sargent and Ljungqvist (1995, 1999, 2000).

## Growth accounting

$$
\begin{gathered}
Y_{t}=A_{t} K_{t}^{\alpha} L_{t}^{1-\alpha} \\
\frac{Y_{t}}{N_{t}}=A_{t}^{\frac{1}{1-\alpha}}\left(\frac{K_{t}}{Y_{t}}\right)^{\frac{\alpha}{1-\alpha}}\left(\frac{L_{t}}{N_{t}}\right)
\end{gathered}
$$

Note: On a balanced growth path, the capital-output ratio, $K_{t} / Y_{t}$, and hours per working-age person, $L_{t} / N_{t}$, are constant.

## Great Depressions methodology

Cole and Ohanian (1999), Kehoe and Prescott (2002)

Aggregate production function:

$$
Y_{t}=A_{t} K_{t}^{\alpha} L_{t}^{1-\alpha} .
$$

Balanced growth path:
Suppose that $A_{t}=A_{0} g^{(1-\alpha) t}$. When the capital-output ratio, $K_{t} / Y_{t}$, and hours per working-age person, $L_{t} / N_{t}$, are constant, output per working-age person, $Y_{t} / N_{t}$, grows at constant rate $g-1$.

Measure output growth with respect to the balanced growth path.

- Trend growth represents the stock of useable production knowledge growing smoothly over time.
- This knowledge is not country specific.
- Countries grow at the same rate, $g-1$, on different balanced growth paths.
- Levels differ across countries because institutions (such as taxes) are different.
- Changing institutions moves the country to a different balanced growth path.
- Take $g-1$ to be growth rate of the industrial leader - United States: $g=1.02$

Real GDP per Capita in the United States


## Growth accounting

$Y_{t}:$ real GDP (national income accounts - SNA93, 1954-2000)
$X_{t}$ : real investment (national income accounts)
$L_{t}:$ hours worked (labor surveys, 1959-1980, 1977-2000)
Construct capital stocks:

$$
K_{t+1}=(1-\delta) K_{t}+X_{t}
$$

Total factor productivity is the residual:

$$
A_{t}=Y_{t} / K_{t}^{\alpha} L_{t}^{1-\alpha}
$$

Growth Accounting for Spain 1960-2000


Growth Accounting for the United States 1960-2000


Work in Spain 1960-2000


Hours Worked per Working-Age Person


## Something happened in Spain starting in 1975!

End of the dictatorship

Acuerdos de Moncloa

Instead of focusing on lots of institutional changes, we are going to see how far we can go in accounting for Spain's growth experience after 1975 by incorporating tax changes in a simple, one sector general equilibrium growth model.

Growth Accounting for France 1960-2000


## Model

Stand-in consumer:

$$
\max \sum_{t=1970}^{\infty} \beta^{t}\left[\gamma \log C_{t}+(1-\gamma) \log \left(N_{t} \bar{h}-L_{t}\right)\right]
$$

$$
\begin{aligned}
& \text { s.t. }\left(1+\tau_{t}^{c}\right) C_{t}+K_{t+1}-K_{t} \\
& =\left(1-\tau_{t}^{\ell}\right) w_{t} L_{t}+\left(1-\tau_{t}^{k}\right)\left(r_{t}-\delta\right) K_{t}+T_{t} . \\
& K_{1970}=\bar{K}_{1970} .
\end{aligned}
$$

Feasibility:

$$
C_{t}+K_{t+1}-(1-\delta) K_{t}=A_{t} K_{t}^{\alpha} L_{t}^{1-\alpha} .
$$

Government budget constraint:

$$
\tau_{t}^{c} C_{t}+\tau_{t}^{\ell} w_{t} L_{t}+\tau_{t}^{k}\left(r_{t}-\delta\right) K_{t}=T_{t} .
$$

## Calibration

$\delta=0.044\left(\delta K_{1970} / Y_{1970}=0.091\right)$
$\alpha=0.300$ (Gollin (2002), European Economy (1994))
Tax data: Boscá, Fernández, and Taguas (1999), 1965-1996, and ours, 1996-2000, using methodology of Mendoza, Razin, and Tesar (1994).

Income tax rates: marginal > average (by a factor of 1.8) (Calonge and Conesa (2003)).

Parameters of stand-in consumer's utility function $\beta$ and $\gamma$ : estimated using 1965-1974 data.

First order conditions:

$$
\begin{aligned}
& \beta=\frac{\left(1+\tau_{t+1}^{c}\right) C_{t+1}}{\left(1+\tau_{t}^{c}\right) C_{t}} \frac{1}{1+\left(1-\tau_{t}^{k}\right)\left(r_{t}-\delta\right)} \\
& \gamma=\frac{\left(1+\tau_{t}^{c}\right) C_{t}}{\left(1+\tau_{t}^{c}\right) C_{t}+\left(1-\tau_{t}^{\ell}\right) w_{t}\left(N_{t} \bar{h}-L_{t}\right)}
\end{aligned}
$$

## Numerical experiments

Set $K_{1970}=\bar{K}_{1970}$. Set $A_{t}=Y_{t} / K_{t}^{\alpha} L_{t}^{1-\alpha}, t=1970, \ldots, 2000$.

1. Constant taxes - set taxes $\tau_{t}^{c}, \tau_{t}^{\ell}, \tau_{t}^{k}$ equal to values in 1975. Estimate $\beta=0.973, \gamma=0.351$ for 1965-1974 data.
2. Taxes - set taxes equal to their actual values 1970-2000. Estimate $\beta=0.970, \gamma=0.333$ for 1965-1974 data.

Marginal Tax Rates in Spain


Detrended Real GDP per Working-Age Person in Spain


Hours Worked per Working-Age Person in Spain


Capital/Output Ratio in Spain


## Results

The model with constant taxes fails to account for the sharp fall in hours worked per working-age person after 1975.

The model with taxes accounts for more than 80 percent of the fall in hours worked between 1974 and 1994. (Hours worked per working-age person falls 41 percent in the data and 35 percent in the model.)

The model fails to account for the rapidness of the fall in hours worked between 1974 and 1985.

The model fails to account for the partial recovery in hours worked after 1994.

## Comments

High elasticity of labor supply implicit in logarithmic utility function: and Hansen (1985) and Rogerson (1987).

Calibrated values of $\beta$ and $\gamma$ implicitly take into account different institutions. The assumption is that these stay constant over time.

There is a lot left out of the model!
This macro analysis points to the directions in which we need to do more micro analysis.

## An instructive comparison: France

Calibrate:
$\beta=0.993, \gamma=0.394$ in model with constant taxes.
$\beta=0.991, \gamma=0.386$ in model with actual taxes.
$\alpha=0.300, \delta=0.046$.
The model does an impressive job in accounting for the evolution of GDP, hours worked, and the capital stock.

Prescott (2002)

Marginal Tax Rates in France


Real GDP per Working-Age Person in France


Hours Worked per Working-Age Person in France


Capital/Output Ratio in France


## Sensitivity Analysis

$$
\sum_{t=190}^{\infty} \beta^{t}\left(\left[\left(\frac{C_{t}}{\tilde{N}_{t}}\right)^{\gamma}\left(\frac{N_{t} \bar{h}-L_{t}}{N_{t}}\right)^{1-\gamma}\right]^{\phi}-1\right) / \phi
$$

where $\tilde{N}_{t}$ is adult-equivalent population and $\phi=-1$.
Calibrate:
$\beta=0.987, \gamma=0.351$ in model with constant taxes.
$\beta=0.984, \gamma=0.333$ in model with constant taxes.
The model does better in accounting for the evolution of hours worked, but worse in accounting for capital accumulation.

Detrended Real GDP per Working Age Person in Spain


Hours Worked per Working Age Person in Spain


Capital/Output Ratio in Spain


## Where could we go from here?

Disaggregated models of labor market

- different behavior along education/gender/age dimensions Jiménez-Martín (1998), Jiménez-Martín and Sánchez Martín (2003), Sanchez (2002)
- different behavior along sectoral dimensions Marimon and Zilibotti (1998)

Changes in institutions - Acuerdos de Moncloa, labor market reforms

Changes in taxes cannot be left out of the story!

